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# TREATISE 

ON

## LOGIC,

ON THE BASIS OF ALDRICH,<br>WITH ILLUSTRATIVE NOTES.

## BY <br> THE REV. JOHN HUYSHE, M.A.

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It is to be hoped that those academical bodies who have been wise enough to retain this science, will, instead of being persuaded to abandon it, give their attention rather to its improvement and more effectual cultivation.

Dr. Whately, Elements of Logic, Preface, ad finem.

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## PREFACE.

The present treatise is intended to assist those who wish to study Aldrich's Logic, in order to pass their examination in the Oxford Schools. The author's sole endeavour has been, to render the study of the science as easy as he could; and he has freely made use of the suggestions of others, whereever he thought that they were calculated to elucidate any difficulty.

With regard to style, he has endeavoured to explain with perspicuity, and not with elegance; for " prolixity of style, homeliness of illustration, and baldness of expression, are to be regarded as blemishes not worth thinking of when any thing is to be gained in respect of clearness."-(Whately's Logic, Preface.)

## A

## TREATISE ON LOGIC.

PART I. SECT. I.

ON THE OPERATIONS OF THE MIND.
There are three operations of the mind- operations of simple apprehension, judgement, and discourse or reasoning.
Simple apprehension is the mere intellectual simple ap. conception of a thing. It is sometimes termed perception, because the apprehension of the mind was thought to be analogous to per-to what ception by the senses; thus it was imagined that, by apprehension, an idea of any object was imprinted on the mind, just as its image was, by sight, on the eye. The result of this iss result. operation is properly termed a notion, or, metaphorically, an image, idea, representation, or conception.

There are two kinds of simple apprehen- Two kind. sion, viz. incomplex and complex.


B

Incomplex apprehension.

Simple incomplex apprehension is the conception of one object, or of many taken confuse, i. e. without any grammatical relation to each other ${ }^{\text {a }}$. It is by this kind of apprehension that the mind gains the ideas represented by each word, in any sentence, when taken separately.
Complex ap- Complex apprehension is the conception of prehension. several objects taken with a certain order and reference to each other. And it is by this kind of apprehension that the mind understands the meaning of all the words of a sentence taken collectively-or, in other words, the complex idea which that sentence may intend to convey.

Of these two kinds of apprehension, the incomplex is prior in point of time.
Judgement. Judgement ${ }^{\text {b }}$ is the decision on the agreement or disagreement of any two objects when

[^0]compared with each other; and until this decision is made, judgement cannot be said to be formed.
There are two kinds of judgement, affrma- Two kinds tive and negative.

Affirmative judgement (which is also termed composition) is that which expresses the agreement of the two objects which were compared.

Negative judgement, or division, expresses their mutual disagreement.

The copula is that which indicates the act Copula. of judgement, viz. it serves to express the agreement or disagreement of two objects. It is the substantive verb alone in its present tense; and is either affirmative or negative.

It is by deciding whether the affirmative Diference copula est, or the negative non est, should jangement be applied, that judgement differs from com- apprehenplex apprehension: for the mere act of understanding the sense conveyed by any assertion, whether affirmative or not, is the office of complex apprehension; but in judgement, the mind not only understands the meaning of the assertion, but, by determining the copula, shows that it acquiesces in, or dissents from, that assertion.
Since the copula serves to indicate the Ue of the copula.

[^1]agreement or disagreement of two objects, it is obvious that the affirmative copula expresses their agreement, and the negative their disagreement. Thus, "The soul is immortal," is an affirmative judgement, and "The earth is not stationary," is a negative judgement.
Reasoning. Reasoning, or discourse, is the motion or progress of the mind from one or more judgements to another resulting from them. It is also termed ratiocination ${ }^{c}$; and it is expressed or signified by some illative, viz. inferential particle, as hence, therefore, consequently, \&c.; thus,

Nemo mortalium omnibus horis sapit :
Ego sum mortalis :
Ergo, Non omnibus horis sapio.

The mental operations liable to defects.

Owing to the weakness of human nature, the mind of man is fallible, and its operations are consequently liable to certain errors or defects. The error incidental to apprehension is termed indistinctness, that of judgement, falsity, and of reasoning, " a faulty mode of

[^2]inferringd." Thus man's ideas of eternity, ons- Instances nipore, infinity, must be in $\mathrm{S}_{\mathrm{o}}$ if If these dewere to decide that "the sun moves round the earth," my judgement would be false; and if from these two judgements, viz. "Qui sapit pauca loquitur" and "Pauca loquor," I were to deduce this third judgement, "Sapio," the inference would be erroneous.

In order to obviate these defects, certain why logic rules have been laid down, the knowledge of was aaght. which is termed logic, or the art of reasoning. It is defined to be "ars instrumentalis dirigens Looici de mentem in cognitione rerum;" for logic, when applied to practice ${ }^{e}$, becomes an art; and since an art: it is not studied for its own sake, but with a view to some ulterior object, it is not a final or master art, but an instrumental or subordinate

[^3]its object: art. The object which logic has in view, is, " to direct the mind in the attainment of knowhowatained. ledge ${ }^{f}$," and the means which it adopts to attain that object are, "the showing the proper use of words:" for since, in reasoning, terms may be indistinct, propositions false, and arguments. fallacious; hence, by remedying these defects, i.e. by shewing the proper use of language, logic does guide and direct the mind in the attainment of knowledge.

[^4]Since there are three operations of the mind, Three parts and consequently three defects to correct, hence also there are three parts of logic.

## SECTION II.

In order to express these operations of the origin of mind, and to communicate them to each other, men were compelled to invent certain signs or tokens, which are called words; a knowledge of the proper use of which must be necessary, in order that the mental operations may not be defective.

A word is defined to be, "Signum rei vel Defnition conceptûs ex instituto vicarium;" i.e. "An of a word. arbitrary vicarious sign of a thing or idea ${ }^{\text {g }}$."

1. A word is a sign, i. e. it is a token of the A word is a existence of some thing or idea meant to be represented by it.
2. A word is the sign of a thing, because it A word is the does serve to represent the particular object ining.

[^5]which that word conveys to the mind of the hearer.

The sign of an idea.

A vicarious sign.

An arbitrary sign.

Natural sonnds are not words.

Three kinds of words.
3. A word is the sign of an idea, because a word, when uttered, conveys the very same idea to the hearer's mind which the speaker had in his own.
4. A word is a vicarious sign, inasmuch as it not only conveys the idea of an object, but it supplies the place of that object, or " primo declarat conceptum, deinde supponit pro re ${ }^{\mathrm{h}}$," i. e. a word first declares the idea or conception of any object intended, and afterwards acts as a substitute for that very object itself.
5. A word is also an arbitrary sign, for it requires the mutual agreement of men in order to acquire any signification.

Sounds, therefore, which are suggested by nature, such as sighs, groans, shrieks, \&c. are not words, for they are not formed "ex instituto."
As there are three mental operations, there are three kinds of words expressive of them : those which express simple apprehension are called simple words, those which express judgement, complex ${ }^{i}$, those which express discursus, decomplex.

[^6]Every decomplex word consists of three complex, and every complex word of three simple words; for a complex word, which is commonly called a proposition, consists of, 1 . The subject, Component i. e. "that concerning which something else is proposition. said;" 2. The predicate, i.e. "that which is said of another;" and 3. The copula, which comes between the subject and predicate. It frequently happens that these three words are united in one, e.g. "Loquor," viz. "Ego sum loquens;" or the copula is joined to the predicate, as " Cats eat mice," i. e. "Cats are animals which eat mice;" or they may be composed of a great number of grammatical words, as "The opening of this epistle exhibits a connexion with the history which alone would satisfy my mind that the epistle was written by St. Paul, and by
expressive of discursus must be a certain combination of complex words, hence it is termed decomplex, i. e. doubly complex.
$k$ " It is proper to observe, that the copula, as such, has no relation to time, but expresses merely the agreement or disagreement of two given terms : hence, if any other tense of the substantive verb, besides the present, is used, it is either to be understood as the same in sense, (the difference of tense being regarded as a matter of grammatical convenience only;) or, else, if the circumstance of time really do modify the sense of the whole proposition, so as to make the use of that tense an essential, then, this circumstance is to be regarded as a part of one of the terms: at that time, or some such expression being understood. Sometimes the substantive verb is both copula and predicate; i. e. where existence only is predicated : e. g. Deus est."-Whately.

St. Paul in the situation in which the history places him." The whole of this sentence consists of but one proposition; the subject of which is, "The opening of this epistle:" the copula " is," and "an opening which exhibits a connexion," etc. is the predicate.

Subject and predicate are sometimes transposed.

The subject ought to be the first word in every proposition, and the predicate the last; but this verbal arrangement is sometimes changed ${ }^{1}$ : thus in the following examples, the predicate stands first in the propositions; and the grammatical words which compose the subject and predicate are united by a hyphen, the subject, predicate, and copula being separated by an asterisk.

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" Blessed * are the - poor - in - spirit."
" Faded * is * the - flower - which - once - decked - her -
    fair - bosom."
" Apex - senectutis * est * amicitia."
" Varius - et - multiplex * est * auctoritas."
" Ai\sigma\chipo\nu * '̇\sigma\tau\iota * \tau\delta - \psi\epsilonv\delta\\hat{\eta}-\lambda\epsiloń\gamma\epsilon\omega\nu."
```



Subject, predicate, and copula, are always three in sense.

These three words, though (as it has been shown) they are not always three in number, are always to be considered as three in sense.

[^7]
## ON THE DIVISIONS OF NOUNS.

Since the subject and predicate are, as far as Termo of a . regards the sense, the extremes of a proposition; hence they are called "the terms," from the Latin word "terminus."

The first part of logic is, therefore, said to with what
 simple apprehension; the second part treats of engaged. complex words or propositions, which express judgement; and the third part, of decomplex words or syllogisms, which express reasoning.

## SECTION III.

Simple words are of three kinds, categore- Division or matic, syncategorematic, and mixed. Catego- $\begin{gathered}\text { iimpopee } \\ \text { Cortegre }\end{gathered}$ rematic words, which are also called simple malict. terms, are such as may be used alone, either as the subject or predicate of a proposition. And such words are nouns substantive in the nominative case, as well as verbs in the infinitive mood; which (see Dr. Whately) are properly nouns substantive. No nouns, therefore, in the oblique cases can be categorematics. ${ }^{\text {m }}$

[^8]Syncategorematics. can form only a part of the subject or predicate, as adjectives, nouns in oblique cases, verbs, and other parts of speech; for though an adjective is often used as the predicate of a proposition, yet some substantive must always be considered as understood and implied, though not expressed ${ }^{\text {n }}$.
Misedwords. Mixed words are such as are formed by some combination of the two other species; and of these there may be three classes, examples of which are given in Aldrich (c. 1. § 3.), the first, " semper," being compounded of two syncategorematics ; the second, " nemo," of a categorematic and a syncategorematic; and the third, "currit," of a syncategorematic and the copula, Grammatical to which last class all grammatical verbs may be verbs are vised mords. referred; ; for they may all be resolved into the
med copula and the participle: thus, "I walk" is

[^9]equivalent to "I am walking." "Moneo," i. e. How reolv"Ego sum monens," " $\gamma \rho a ́ \phi \omega$ " is equivalent to ${ }^{\text {able. }}$


There is but one verb in logic, which is the the logical copula, the substantive verb in the present tense.
The logical noun ${ }^{\circ}$ is defined to be "terminus Defnition of simplex sine tempore significativus;" i.e. a a the ev. ${ }^{\text {teical }}$ logical noun is "a word which is significant, and has no reference to time ${ }^{\mathrm{p}}$; that is, it is equivalent to a categorematic word. Adverbs, conjunctions, \&c. are not, therefore, logical nouns; for they have not any actual signification, but they serve to qualify those nouns to which they are joined.

There are many divisions of logical nouns, Disivion three of which are most necessary to be observed ; viz. the common, univocal, and noun which mot of the second intention, because the union of necesary. these three forms what is termed "a predicable."
The first division of nouns is into singular and $\begin{gathered}\text { Singiar and } \\ \text { nomion }\end{gathered}$ common ${ }^{9}$.

[^10]The singular noun speaks of individuals alone, the common noun of a whole class of individuals, and is applicable to every individual of that class, inasmuch as it comprehends them in its signification : thus " Oxford," "London," "Bristol," are singular nouns, because they express or stand for individuals; and "city," "town," \&c. are common nouns, and they not only represent the whole class which they express, but are likewise applicable to "Oxford," "London," "Bristol," \&c.; which are individuals comprehended in those classes.
division of nouns, inasmuch as it comprehends the whole class; for every noun must either be singular or common. The other divisions are not so much the divisions of nouns, as the different modes of employing the same noun. For " the usual divisions of words into univocal, equivocal, and analogous, and into words of the first and second intention, are not, strictly speaking, divisions of $w o r d s$, but divisions of the manner of employing them : the same word may be employed either univocally, equivocally, or analogously; either in the first intention or in the second. The ordinary logical treatises often occasion great perplexity to the learner by not noticing this circumstance, but rather leading him to suppose the contrary."-Whately.

Thus, for instance, the word " bull" may be used equivocally; for it may signify " an animal" or " $a$-blunder in an expression," two ideas which apparently have not any analogy to each other: so when considered as meaning " an animal" only, it will be univocally used; for then its one signification, which is that of an animal, will be applicable in the same sense to many objects. Again, when it is used to signify " a violent enemy," it is used analogously; this signification being derived from the analogy between " a bull" (the animal) and " a violent enemy," who seems to partake of the disposition of such an animal.
N. B. Every thing which has actual existence is represented by a singular noun; a common noun does not represent a thing which has actual existence, but an idea or nature common to many individuals; i. e. that idea which is the result of the abstractive faculty. [See Section IV.]

A common noun may be considered as sin- Common gular when a sign of singularity is affixed to it, nonns used as thus: " He is gone to the river," meaning the Isis. "River" would here be considered as a singular noun, because its signification applies to but one object. So also a singular noun might singular be employed as common, by extending its signi- ploged as fication to many individuals. "The Cesars common. were emperors of Rome."

A definite noun is such as has not the particle Definite and non ${ }^{r}$ prefixed to it. The indefinite is that to indefini. which the particle non is prefixed. Thus "That quadruped is not a dog:" dog is here used indefinitely; for since it is predicated of that certain quadruped that it is not a dog, the class $d o g$ alone is excluded, and it remains wholly undefined to what other class of quadrupeds it may belong.

The positive noun speaks of a thing as it Prositive, and negative nouns.

[^11]were present; i.e. possessed by any subject. The privative denotes the absence of a thing from a subject capable of possessing it; and the negative denotes the absence of a thing from a subject incapable of possessing it. Thus "rational" is spoken positively, "unlearned" privatively, of man; and "irrational" is spoken negatively of brutes.

Again, Positive, A man of sense.<br>Privative, A senseless boy. Negative, A senseless stone.

Univocal uouns.

Equivocal nouns.

An univocal noun ${ }^{8}$ is that which has but one signification, and in that one signification is equally applicable to many objects.

An equivocal noun has more than one signification, and in each signification is equally applicable to many objects: such as post, bull, mail, \&c. Such words are an imperfection in a language; for the same sound is intended to convey two distinct ideas, the result of which must be frequent mistakes.

[^12]Analogous nouns are such as have but one Analogous significtion; but in that one signification they ${ }^{\text {nonas. }}$ signification, but in that one signification they are unequally, viz. with unequal propriety, applied to many things. When any objects are united by some resemblance which they bear to each other, the same word is often used to apply to them, which word is called analogous; as "a vein in the body," and "a vein of metal;" where the resemblance is obvious. Analogous nouns are also used to represent any two or more objects which have no resemblance to each other; as, "a sour apple," and "a sour look;" though even in this instance some analogy may be perceived in the ideas conveyed by these words.
Concrete nouns are such as express some Concrete quality, at the same time implying the subject in which that quality exists; as prudent, wise ${ }^{\text {t }}$.
Abstract nouns express a quality by itself, and, Abetract as it were, independent of the subject possessed ${ }^{\text {nonns. }}$ of it; such as prudence, wisdom.
Concrete nouns are not always adjectives ${ }^{\text {u }}, \begin{gathered}\text { Concreves } \\ \text { nadeens } \\ \text { adectives }\end{gathered}$
: Prudent is a concrete noun, because it cannot be used without at the same time implying or referring to the being who is possessed of that quality: but prudence is an abstruct noun, and may be used without any reference whatsoever to the subject which is possessed of it; it is a word which expresses an abstract idea.

- It may perhaps be questioned whether all concrete nouns are not strictly adjectives, though substantively used: but this is a question of no importance, as far as regards logic. It has before been shown, that the same word may be used univocally,
although most frequently so: e. g. fool, philosopher, astronomer, geometrician, \&c. which are concretes; the abstracts to them being folly, philosophy, astronomy, geometry, \&c.
Abolate and An absolute noun is that whose sense is comrelative nouus. plete in itself; and does not imply a relation to any other thing. The relative noun implies the idea of its correlative, as husband, which implies the idea of wife.
Agreeing and opposite nouns.

Nouns of first and second intention.

Agreeing nouns are such as express qualities which may be said of any one object at the same time, as " a horse may be both swift and tractable." Opposite nouns express qualities which cannot be said of any one object at the same time: thus " a horse could not be said to be at the same time both swift and slow." At different times opposite nouns may be predicated of the same object: thus " $a$ horse may be said to be tractable to-day, and intractable to-morrow."
The first intention ${ }^{\mathrm{x}}$ of a word is its common signification; i.e. its vague colloquial meaning. Its second intention is its strict and definite
equivocally, and analogously: so also the same word may be considered as relative, opposite, \&c.; e.g. brother is the concrete to fraternity; and it may also be regarded as a relative noun, for it suggests the idea of its correlative sister : so again, great and small are relative nouns; and they may be regarded also as opposite, for they cannot both be predicated of the same thing at the same time : this is the case with many nouns.
x "The first intention of a term, (according to the usual acceptation of this phrase), is a certain vague and general sig-
sense, limited as may be required when it is used in any particular science or art. When, therefore, we speak logically, all words are limited in their signification, and may consequently be considered as in their second intention. As the same word may be used in many different sciences and in different significations, it is evi- Many second dent that such a word will have as many second $\begin{gathered}\text { intentiond } \\ \text { the } \\ \text { warde }\end{gathered}$ intentions as there are sciences in which it is used: thus the word triangle in mathematics is "a plane rectilineal figure contained by three straight lines;" but in music it signifies "a musical instrument.' All second intentions bear a resemblance, in part of their signification, to the primary or first intention.

Care must be taken not to confound the logical Etymological first and second intention with the etymological; second for the etymological first intention of a word is that meaning which most nearly approaches to the root of that word; any deviation in
nification of it, as opposed to one more precise and limited, which it bears in some particular art, science, or system, and which is called its second intention. Thus, among farmers, in some parts, the word beast is applied particularly and especially to the ox kind; and bird, in the language of many sportsmen, is in like manner appropriated to the partridge: the common and general acceptation (which every one is well acquainted with) of each of those two words, is the first intention of each; the other is its second intention."-Elements of Logic. In fact, any word which is applied in a limited sense, in an argument, will be used in a second intention.
signification from which would be termed its etymological second intention.

## SECTION IV.

Of singular. A singular noun ${ }^{y}$ is also termed in logic indivisible, because it is incapable of being logically divided, inasmuch as its signification extends to one object, and one only; i.e. its object is numerically one: but nevertheless whatever can be called one, is not therefore necessarily singular; for many things, which possess any common quality, may (as far that resemblance goes) be considered as one in sense though not one in

[^13]number; and thus one common name may be assigned to them, which (as far as they resemble each other) will be applicable to any one or to all of them. This operation is termed abstraction $^{2}$, Abstration. which is defined to be "that faculty of the mind Its defnition. by which, in the contemplation of many singulars or individuals, it neglects all those points in which the singulars differ from each other, regarding those only in which they agree." The its reant. result of such an operation is an abstract idea; i. e. the idea of an universal nature which extends over many individuals, not being different in each, but the same in all. Hence it is termed universale, or ens unum in multis. The word

[^14]expressive of such an abstract idea is termed a A predicable. predicable, because such universal nature may be affirmatively predicated of each of those singulars, and of them all collectively. Such a common term ${ }^{\text {a }}$ or predicable is defined to be
Is defnition. "nomen commune, univocum, secunde intentionis;" or, a common, univocal noun of the second intention: for this common noun, although applicable to many individuals, is considered as representative of only one idea; hence it is univocal. And since a word when thus applied is not used in a vague but limited and definite sense, it is also said to be a word of the second intention.

This abstract nature does not denote any really existing thing, nor can it be supposed to exist, unless combined with some singulars: the motive for conceiving it to exist is merely with a

[^15]view to generalization ${ }^{\text {b }}$ and classification. "The object of this operation is the formation of new aggregates, by means either of the generalizing, or of the synthetical faculties."-Bentham, p.57.

## SECTION V.

The essence ${ }^{c}$ of any thing is "that which Essence. makes it to be what it is." If, therefore, it be deprived of its essence, or of any part of it, it no longer exists as it was. This essence is not really-existing, but is an imaginary nature, the notion of which may be resolved into two parts, Its two parts. viz. that part of an essence which is common to it as well as to other essences, which is also called the material part or genus; and that part Material part
b "Generalization implies abstraction, but it is not the same thing, for there may be abstraction without generalization; when we are speaking of an individual, it is usually an abstract notion that we form; e.g. suppose we are speaking of the present king of France; he must actually be either at Paris or elsewhere; sitting, standing, or in some other posture; and in such or such a dress, \&cc. Yet many of these circumstances, (which are separable accidents, and consequently) which are regarded as non-essential to the individual, are quite disregarded by us; and we abstract from them what we consider as essential; thus forming an abstract notion of the individual. Yet there is here no generalization."-Whately.
e Essence is the nature of anything, even though that thing has not any existence : thus a lily in winter has an essence, but in summer it has existence also.
which is not common to any other essence, but is peculiar to this one essence, and distinguishes - it from all others, and constitutes it what it is. This part is called the formal or characteristic Formal part
ordifferentia. part, i. e. the differentia. Thus a triangle is " a plane figure contained by three sides." The common or material part of the essence of triangle, viz. its genus, is " a plane figure," which is common to squares, circles, oblongs, \&c.; but its being "contained by three sides," is the characteristic part of its essence, viz. its differentia; for it constitutes the distinction between a triangle and any other figure whatsoever ; for no figure can be a triangle which is not contained by three sides, nor can any three-sided figure be any thing but a triangle.
Species. The whole of any essence is called the species; hence it is evident, that every species is made up by the union of the genus and differentia; for every

Genus and differentia make up the species. e.g. by uniting the two parts, "a plane figure," (the genus,) and "contained by three sides," (the differentia,) we form triangle, which is a species of figure.

Qualities joined to an essence.

To any essence different qualities may be observed to be joined; and of such qualities there oftwokinds. may be two kinds, for they may either be necessarily joined to the essence, or only contingently, i. e. accidentally. Such as are necessarily joined
to any essence are termed properties, and such Prorerties. as are only contingently or accidentally joined are called accidents; e.g. "the having three Accidents. angles" is a property of a triangle, for it necessarily accompanies its essence; or, as Dr. Whately says, it is " the result of the differentia." So " the being equilateral, rightangled," \&c. are accidents to a triangle, for such qualities do not of necessity belong to triangles; the absence of which would not affect the essence or species; for "every accident must be separable from the species, else it would be a property ${ }^{\text {d." }}$

[^16]Five heads of predicables.

From the foregoing considerations, it is manifest that there can be but five heads of predicables; for whatever can be asserted of many things, must be predicated either as their whole essence, or as a part of their essence, or as joined to their essence-whence will arise these five heads ${ }^{e}$.

1. Species, or the whole essence.
2. Genus, or the common part of the essence.
3. Differentia, or the formal part.
4. Property, or something necessarily joined to the essence.
5. Accident, or something accidentally joined to the essence.

These predicables, therefore, are predicated or asserted of those things in which there is supposed to exist that abstract nature of which such
always one quality, but is frequently compounded of several together, no one of which would alone suffice." For the distinction between a property and an accident, see note n .

- It should be borne in mind, that each of these heads of predicables are relative terms ; for that which is a genus if predicated of some things, will be a species when predicated of others, or a property or an accident, \&ce.; for " we cannot say what predicable any term is, or whether it is any at all, unless it be specified of what it is to be predicated: e. g. the term red would be considered a genus in relation to the terms pink, scarlet, 8 cc .; it might be regarded as the differentia, in relation to red-rose; as a property of blood; as an accident of a house," \&c. - Whately.
predicable is the representative. Thus the genus (which is the material or common part of many essences or species) is predicated of many things differing in species; i. e. it is predicated of those different species which it includes under its more extensive signification. Thus figure is predicated of triangles, circles, squares, \&c. which differ in species. But species is predicated of things differing from each other in number; i. e. of those individuals, each of which possesses an essence signified by the word which expresses the species.
The other three heads of predicables, viz. differentia, property, and accident, are predicated of things differing as well in number as in species; because they have a relation either to a genus or a species. If to a genus, they can be predicated of all the species which that genus contains; and if they have a reference to a species, they can be predicated of all the different individuals of that species.
Genus and species are commonly said to be predicated in " quid;" thus if the question be asked "Quid est illud?" the answer must be returned by stating its genus or species. Difference is predicated in " quale quid," and property and accident in "quale." Hence we may easily form the usual definitions of the five heads of predicables ${ }^{f}$.

[^17]Definition of genus.

Genus is a predicable predicated in "quid," of many things differing in species, as the material or common part of their essence.
ofdiference. Difference is a predicable which is predicated in "quale quid," of many things differing either in number or in species, as the distinguishing part of their essence.

Of species.
Species is a predicable which is predicated in "quid," of many things differing in number, as the whole of their essence.

Of property.
Property is a predicable which is predicated in "quale," of many things differing in species or in number, as necessarily joined to their essence.

Of accident.
Accident is a predicable which is predicated in "quale," of many things differing in species or in number, as contingently joined to their essence.
Genus a logicalwhole.

Genus is called a logical wholeg, because it is the most comprehensive term in its signifi-
universal are not one and the same, for the former is the sign expressive of the latter: the predicable is that which is asserted of many, and the universal is one nature existing in many.
$g$ A logical whole is that term which has the most extensive signification; a metaphysical whole is the most comprehensive term. Hence genus is a logical whole, for it contains the species; but species is a metaphysical whole, inasmuch as it implies the genus. Genus expresses a less comprehensive idea than species, for the species denotes the whole essence; i. e. a complex idea, formed by the union of the less complex notions of the genus and the difference.
cation, and contains species as its subject parts; viz. includes it under its own more extensive signification; for the genus may be affirmatively predicated of all its contained species, e. g.
All $\left\{\begin{array}{l}\text { Men } \\ \text { Beasts } \\ \text { Birds } \\ \text { Fishes } \\ \text { Insects }\end{array}\right\}$ are animals.

Thus animal is the logical whole, and men, beasts, \&zc. are its subject parts.

Species, being the whole essence, necessarily speie a implies the genus, which is a part of that es- whole. sence; it is a more complete and comprehensive term than genus, and is therefore termed a metaphysical whole; e.g. man is a metaphysical whole, and implies rational animal.
The difference is said to divide the genus, Diference because when added to the genus it forms dif gene and ferent species, and thus divides, as it were, the tie species. genus into its subject species; and, as the difference when added to the genus makes up the species, hence it is said to constitute the species, inasmuch as it completes its essence.
The following Table presents at one view the heads of Predicables, with their subdivisions.


## SECTION VI.

There are two kinds of genus; viz. genus $\begin{aligned} & \text { Two kind of } \\ & \text { genat. }\end{aligned}$ summum and genus subaltern.
There are also two kinds of species; viz. Two kinds 0 species subaltern and species infima.

Summum genus ${ }^{\text {l }}$ cannot be the subject of any sumnum cognate genus. It is the highest and most extensive term that can be imagined, and there is not any superior genus under which it may be classed: it is, in short, the most abstract notion that the human mind can conceive, and may be

[^18]affirmatively predicated of every idea and every object.

Infima species.

Cognate genera, and species.

Subaltern genera, and species.

Infima species may be the subject of every cognate genus. It is the first common nature which is the result of any abstraction ; it cannot be considered as a genus with reference to any thing, but is considered as composed of individuals only.

Cognate genera and species are such as result from repeatedly abstracting the differences which are perceived to exist in the same individuals, and regarding those abstract notions in which they agree: thus corporeal, animate, sensitive, \&c. are said to be cognate to man, and inanimate, insensilive, \&c. cognate to stones.

There is no actual difference between subaltern genus and subaltern species; the difference is only relative: the former may be predicated of a cognate species, and the latter may be the subject of a cognate genus: they are those intermediate genera and species which are supposed to exist between summum genus and any infima species; each of them may be regarded as a genus with reference to all the species below it, and as a species when referred to the genera above it.

The following table may serve to represent, at one view, what has before been said respecting genus and species, with their subdivisions:

Summum genus is that which can never be regarded as a species;
Infima species can never be regarded as a genus;
Subaltern genus may be considered as a subaltern species.
Subaltern species may be considered as a subaltern genus.
There are two kinds of difference, viz. generic $\mathrm{Two}_{\text {wifo }}$ kind of and specific.
Generic difference ${ }^{i}$ is that which constitutes Generic. subaltern species. It is termed generic, because that species which it constitutes may be considered as a subaltern genus; and consequently the generic difference can be affirmatively predicated of every species which is comprehended
${ }^{1}$ The difference and specitic property are often difficult to distinguish from each other ; but it should be remembered, that a property is only joined to an essence, and results therefore from the difference; whereas the difference is a constituting part of the essence. If then a part of any essence be supposed to be taken away, that essence can no longer remain as it was. The following test, therefore, which we may apply in order to find the difference, will, I believe, in most cases succeed. Since the genus and difference, united, form the species, it follows that, if the difference be supposed to be taken away from any species, that species must revert to its subaltern genus: in fact, the species will not any longer exist; but if a property be supposed to be taken from it, the essence, i.e. the species, will not thereby be injured : this test, however, is by no means unerring, but is frequently applicable. Thus "a proposition" is said to be " a rentence which asserts;" hence any sentence which does not assert, (i. e. affirm, or deny), is not a proposition.
c 3
under it: hence it is predicated of things which differ from each other in species; e. g. sensitive is a generic difference to man, and it may be predicated of all animals as well as of man.

Specific difference is that which constitutes infima species; and it is this kind which is generally meant by the logical difference: it can be predicated of all the individuals contained under the species which it constitutes, and is therefore said to be predicated of things which differ in number, i. e. numerically. Thus rational, which is the specific difference of man, is predicable of every man, but not of any other animal.

Property of twokinds: ‘ Generic:

Property is divided into two kinds, viz. generic $^{\mathbf{k}}$ and specific. Generic property is that which is necessarily joined to, or accompanies the essence of the summum or subalSpecific. tern genus. Specific property is that which flows, or results from the essence of the infima

[^19]species, and is predicated of one species and its different individuals, whereas generic property is predicated of different species. Property Poorrold has also been divided into four kinds:
division of property.

1. That which is peculiar to one species, but does not universally belong to its individuals.
2. That which is predicable of the whole species, but not of that species alone.
3. That which may be predicated of all the individuals of a species, and of that species only, but not of it always.
4. That which may be predicated of one species only, of all its individuals and at all times.

Of these four classes, the second is the generic property, and the last, the specific.
The first and third classes cannot strictly be termed properties. Every property must be universal, i. e. it must be applicable to all the individuals of a species, and must belong to that species necessarily, which in the instance adduced by Aldrich, viz. the fact of a man's being a grammarian, cannot be said to be the case, for some men are not grammarians: the third class, for the same reason, cannot be termed a property, even admitting its existence.

Accident is also divided into two kinds, viz. $\mathrm{Two}^{\text {winds }}$ of inseparable and separable.
The inseparable accidents are such as cannot Inseparable: be separated from the individual of whom they
are predicated: thus, if I predicate of a man that " he took a walk yesterday," his having taken a walk would be what is termed an inseparable accident; for though now it cannot be separated from his essence, yet it was only contingently joined to it, and not necessarily.
The separable accident is such as can be separated from the individual; e. g. if I predicate of a man that he is standing, this is a separable accident, for he may sit down.

It should be remembered, that an inseparable accident is predicable only of individuals; for all accidents must be separable from the species, or they would be properties.

## SECTION VII.

Division.

Division ${ }^{1}$ is " the distinct enumeration of the several things signified by a common noun." For as in logic a singular noun is called indivisible, so a common noun is called divisible, because it admits of logical division.
ortwo kindt. There are two kinds of division, i. e. logical
${ }^{1}$ The word " division" literally signifies, " the separation of the component parts of anything ;" in which case each part is absolutely less than the whole divided. But since in logical division the dividing parts are each "in comprehension" greater than the whole divided, hence the word "division," as thus used, is obviously applied in a figurative or secondary sense.
and physical, and, although they are perfectly distinct in their nature from each other, yet logical division is analogous to physical.

Physical division ${ }^{m}$ is the division of an indi- Phyical vidual into its component parts; thus, "a book" divition. viaual into its component parts; thus, " a book might be divided into its leaves, cover, back, \&c.; and it is by this division that any individual object might be divided. Each of the dividing parts in such division is therefore absolutely less than the whole divided.

Logical division is the division of common Lorical nouns, and the whole divided can be predicated of each of its dividing parts ${ }^{\text {n }}$. Thus, "book"
${ }^{m}$ Physical division is the division of individuals, i. e. of objects which have real existence: logical division is the division of ideas : but since an idea itself has not any real.existence, logical division is used upon those words which are the signs of ideas: and common nouns (as has been shown above, Sect. III.) are representatives of ideas, and as such will be the only nouns upon which logical division can operate. Any singular noun may be physically divided, because it represents and stands for one individual object, which may be divided into its component parts.

- A common noun will admit of various modes of division; thus " books" might be divided according to their matter, size, or language, so " animals" may be divided into rational and irrational, cold-blooded and warm-blooded. Hence a logician must bear in mind (what Dr. Whately terms) the principle of division, with reference to his end in view; for "when any thing is capable of being divided in several different ways, we are not to reckon one of these as the true, or real, or right one, without specifying what the object is that we have in view ; for one mode of dividing may be the most suitable for one purpose, and another for another."-Elements of Logic.
might be logically divided into folios, quartos, octavos, \&c. and it might be predicated of all folios that they were books, and of alk quartos, that they were books, \&c. Hence it is manifest, that if the whole divided be a genus, the dividing members must be the species comprehended under it; and if the whole divided be a species, the dividing members must be the individuals contained under that species.

There are three rules for good logical division. 1. Let each of the dividing parts, or any of them, contain less (i; e. have a more limited signification) than the whole divided ${ }^{\circ}$.

The dividing parts imply the whole.

The words minus contineant ${ }^{\mathrm{p}}$, mean that each

- Thus if the word hound were divided into greyhound, dog, bloodhound, \&rc., such a division would err against the first rule, for the word $d o g$ would be more extensive than the whole divided or hound: so, if animal were divided into quadruped and biped, this division would err against the second rule, for the union of these two parts would not be so extensive as animal, the whole divided; for there are many animals which are neither quadrupeds nor bipeds.
p A perfect division may be formed by means of the definite and indefinite nouns, e. g. men may be divided into those who are Europeans and those who are not Europeans; animals, into rational and irrational, bipeds or not bipeds. Such dichotomy, thus produced, by what is called contradictory bifurcation, constitutes a perfect division, for the union of such two parts will obviously be equivalent to the whole divided. If the parts of a divided whole be many in number, such a division may possibly be as complete and perfect as if it were a dichotomy; but it cannot easily be shown to be so, unless the contradictory bifurcate division be applied to it. An instance of this case will be given in the next section.
of the dividing members must be less extensive than the whole divided. For in logical division, each of the dividing parts or members is always more comprehensive ${ }^{\text {q }}$, i. e. has a more extensive signification, than the divided whole : and each of them may thus be considered as more than the whole, inasmuch as they each imply the wholer; for every one of the dividing parts may be regarded as a species, with reference to the whole divided as a genus: thus each of them is a metaphysical whole, when compared with the divided noun, which will be a logical whole to all its dividing parts.

2. Let all the parts collectively be exactly equal to the whole divided.
3. Let the divided parts be distinct, or opposed to each other ; i. e. let not one part be contained

- Aldrich, chap. i. § 7.
= Thus if we were to divide rectilineal figure, we should divide it into triangle, square, circle, \&c., and each of these parts would comprehend more than the whole; for a triangle is not only a rectilineal figure, but it is a three-sided rectilineal figure. The term triangle, therefore, represents a more complex idea than the term rectilineal figure. So the terms square, circle, \&cc. are each more comprehensive than the term rectilineal figure, because they each imply that term. Thus, also, if the whole divided were a species, and its dividing parts were individuals, each of these parts would be a more comprehensive term than the whole: for every singular term, which represents an individual, is a more full and complete term than the species which contains it ; and, since the species may be predicated of each of the individuals under it, consequently each of these individuals implies the species, and is therefore a more comprehensive term.
under another: e.g. if we were to divide tree into forest tree, oak, elm, plum tree, fruit tree, such parts would be contained in each other, for a forest tree may be an oak or an elm, and an elm or an oak is a forest tree.


## SECTION VIII.

Definition.

Its object.

Classes of definition.

Definition", as used in logic, is " an explanatory sentence, i. e. a sentence which explains any term, so as to separate the idea represented by that term from any other idea whatsoever."

A word may be unintelligible to a hearer, either from his not at all understanding its meaning, or from its conveying to his mind an idea, different to that which was intended: the object of definition, therefore, is either to convey to the hearer's mind the idea which the defined term is intended to represent, or else to correct any indistinct notion which may erroneously have been assigned to it.

Definitions are divided into two classes, viz. nominal and real.

* Definition literally signifies " the laying down the boundary of anything:" but it is here used to signify " a sentence which so explains a term, as to separate that term from any other, and thus to lay down (as it were) the boundary or limit of its signification." Since, therefore, it is here used in a peculiar and metaphorical sense, it must be a word of the second intention.


## ON DEFINITION.

The nominal definition explains only the sig- Neminat nification of the term ${ }^{\text {t }}$. Such definitions are used when the term which has been uttered does not convey any idea to the hearer's mind, viz. when he does not understand the meaning of the term, which is therefore explained by making use of some equivalent expression which may be more intelligible: thus you might define emblem, that which is a sign of any thing; or essence, as universal nature; or approximation, as a near approach.

The real definition ${ }^{4}$ is that which declares or Real explains the nature of the term: which professes to explain not only the meaning of the term, but the nature also of the thing signified. Of real definitions there are two species, viz. the acci- ortwo kind. dental and the essenticl.
$t$ "Aldrich having given, as an instance of a nominal definition, the absurd one of ' homo, qui ex humo,' has led some to conclude that the nominal definition must be founded on the etymology; or at least that such was his meaning; but that it was not, is sufficiently plain from the circumstance that Wallis (from whose work his is almost entirely abridged) expressly says the contrary. Be this as it may, however, it is plain that the etymology of a term has nothing to do with any logical consideration of it."-Elements of Logic.

- In many cases the nominal and real essence of anything exactly coincide, viz. the idea conveyed by the word is exactly the same as the nature of the thing : e.g. in mathematics and many other sciences: (see Dr. Whately on this subject). Thus a triangle is "that which has three angles;" and "a rightangled triangle" is " that which has one right-angle," are each both nominal and real definitions.

Accidental definition

The accidental definition is that which defines a term, by describing or enumerating some of its properties or accidents; such definitions are also termed descriptions, and are more commonly to be met with than any others; for as we are frequently unable to ascertain the natural, or component parts of any thing, and more especially the metaphysical parts, i. e. the genus and difference, description is often the only method by which we are able to define a term.

Essential definition.

The essential definition is that which lays down the constituting parts of the essence, and it ortwo kind. is of two kinds, viz. the metaphysical, or logical, and the physical.
Metaphysical The metaphysical definition is that which lays definition. down the ideal parts of an essence, viz. the genus and differentia; hence it is obvious, that any term which will admit of being metaphysically defined, must be a species. No individual ${ }^{x}$, therefore, can be logically defined; neither can summum genus; for it is the highest of all genera, and cannot therefore be defined by assigning its genus and difference, inasmuch as it has not any superior genus : description is the only mode of defining it, i. e. by an enumeration of its properties.

[^20]The physical definition is that which lays Phyical down the real parts of the essence, $i$ e those denition. down the real parts of the essence, i. e. those parts which admit of actual separation; thus horse might be physically defined as being an animal composed of head, body, mane, legs, \&c., and a book, as being composed of cover, back, and leaves ${ }^{\mathrm{y}}$.

There are three rules for good definition.

Rales for definition.

1. "Let the definition be adequate to the term defined;" i. e. the idea conveyed by the definition must be exactly equal to that which is meant to be conveyed by the definitum, or term defined : consequently its signification must not be too extensive, nor too confined. Thus if "a tree" were defined to be " a plant having leaves," such a definition would be too extensive, for many plants have leaves, which are not trees: in this case the definition explains a whole, when the term defined is but a part. Again, if "a tree" were defined to be " a plant which bears fruit;" such a definition would be too limited, for there are many trees which do not bear fruit;
[^21]Definition. $\left\{\begin{array}{l}\text { Nominal, } \\ \text { Real. }\end{array}\left\{\begin{array}{l}\text { Accidental, } \\ \text { Essential. }\end{array}\left\{\begin{array}{l}\text { Metaphysical, } \\ \text { Physical. }\end{array}\right.\right.\right.$
The four infimæ species of definition are nominal, accidental, metaphysical, and physical. This division of definitions is an example of dichotomy. [See the last section.]
and in this case the definition would have explained only a part, when the term defined is a whole.
2. "Let the definition be in itself clearer and more plain than the term defined ${ }^{\text {z." }}$ i. e. the definition must convey an idea which will be clearer and better known to the generality of persons to whom it is addressed, than the idea which is conveyed by the term defined: the words " per se ${ }^{\text {a }}$ " are opposed to " per accidens:" because the term defined may by accident be better understood than the words of the definition ${ }^{b}$.
. 2 It has been frequently objected to metaphysical definition, that it is not clearer (in most cases) than the term defined; and when the term, which is to be defined, is very familiar to the hearer, this certainly is the fact : thus the word man is more familiar to the ear, and is accidentally better known than the term rational animal; but yet the words rational animal are, in their nature, more clear and better known than the word man, inasmuch as they convey less complicated ideas; and all words which express less complicated ideas, are, in their nature, clearer than those which convey more complex ideas. All definitions of ideas purely simple, must of necessity be, at best, not clearer than the terms defined; e.g. the definition of "colour," which could hardly be defined so that the definition should be better known than the term itself.

- See Aldrich, chap. i. § 8.
b Thus, if a triangle were defined to be, "a figure which has its three interior angles together equal to two right angles," such a definition would not be so clear as the word triangle, and would err against the second rule: so, "Old age is the evening of life;" "A warrior is the thunderbolt of war ;" would err against the third rule, for the words which compose these

3. "Let the definition be inclucled in a just number of proper words;" i. e. the words employed must not be used in a metaphorical sense, as such words would probably produce indistinctness : so also the number of the words must be suitable; for too much brevity would produce obscurity, and too great prolixity, confusion.
definitions are metaphorical: again, if we were to define a cascade by saying that it was a waterfall, such a definition would be too short. Care, therefore, must be taken, that all definitions be exactly equivalent or adequate to the terms defined, and that they be, in all respects, more clear and intelligible; for since the difference or essence of a definition is that it be explanatory, it would cease to be a good definition, if it did not render clear and intelligible those terms which before were not so.

## PART II. SECTION I.

Of proposition.

Proposition defined.

The second part of logic treats of proposition or enunciation; i. e. those complex words which are expressive of the second operation of the mind, or judgement.

A proposition is defined to be " oratio indicativa, congrua et perfecta, verum vel falsum significans, sine ambiguitate ${ }^{2}$." This definition is of a compound nature; for it is partly metaphysical, and partly accidental. A proposition would be more accurately defined to be oratio indicativa; i. e. an asserting sentence ${ }^{\text {b }}$. This definition would comprehend the whole essence of proposition ; for "a sentence" is its genus, and " asserting," i. e. affirming, or denying, its difference. The other parts of the former

2 Aldrich, chap. ii. § 1.
${ }^{b}$ A proposition being a sentence which asserts, viz. which affirms or denies; it follows, that all exclamations, interrogations, commands, \&c. are excluded, and are not regarded as propositions : thus, "Do ye now believe ?" "O how amiable are thy dwellings!" "He that made the round world so fast;" are not propositions, since they do not contain any assertion; but " Truth lies in the bottom of a well;" "Tempus fugit;" " Loquor;" "He scattereth the proud in the imaginations of their hearts;" are asserting sentences, and consequently are propositions.
definition are properties, \&c. of proposition, and ought not strictly to form a part of the definition, but to be deduced from it.

There are four requisites for constituting a legitimate proposition.

Four things, requisites for constitnting a proposition.

1. That as far as regards the words, it must be a sentence which affirms or denies ${ }^{\text {c }}$; which is its whole essence.
2. That as to sense, it must signify something true or falsed;" i. e. it must declare that which is the real fact, or that which is not the fact; and this is the property of a proposition.

[^22]3. It must not be an ambiguous sentence; viz. it must not admit of dubious construction, for in this case it would be "orationese;" i. e. it would be more than one sentence, because it would admit of more constructions than one.
4. The sentence must not be ungrammatical, for such a sentence would be unintelligible, and consequently could not be "declaratory!."

## SECTION II.

## Division of propositions.

Substance.

Propositions are divided according to their substance, their quality, and their quantity. The substance ${ }^{8}$ of a proposition is its genus
e Aldrich, chap. ii. § 1.
f These two last rules are self-evident; for if a proposition were ambiguous, viz. admitted of being construed in more ways than one, it would be a sort of double sentence: and this ambiguity may be produced by equivocal words, or by a dubious form of expression; e.g. "That is a bull;" "Crøesus Halyn penetrans magnam pervertit opum vim ;" both these sentences are ambiguous, and may each be considered in more than one way; consequently they may each be regarded as more than one sentence. On this point, see Elements of Logic, chap. iii. § 10. Again, if a proposition were ungrammatical or mutilated, such a sentence might be unintelligible, and would not therefore be a legitimate proposition: this may frequently be observed to be the case in proverbs, and such sort of sentences, where, although the ellipsis is not such as to render the meaning unintelligible, yet it cannot strictly be termed an accurate proposition; for it might produce ambiguity.
s Should not the substance of a proposition be said to be its
or material part of its essence; i. e. its being " a sentence:" and propositions (as regards their substance) are considered as of two kinds: viz. "categorical" and " hypothetical." The categorical proposition is that which asserts Categorical absolutely, i. e. "unconditionally :" e. g. "Be- proposition. nevolence is not the whole of virtue;" "No man can live for ever." The hypothetical is Hypothetithat which asserts under some condition or
whole essence, and not the genus? for every assertion can be expressed either absolutely or conditionally; hence by regarding the substance of propositions, we divide them into categorical and hypothetical, the former of which asserts absolutely, and the latter asserts under some hypothesis, or condition. The substance of a proposition is commonly said to be its genus, or the material part of its essence, viz. that it is a sentence; but if this were the case, commands and questions might also be considered as propositions, which is not the fact. Aldrich says, (chap. ii. § 2.), that to the question "Quce est propositio ?" the answer must be, categorica vel hypothetica; and this is not answering by considering the genus, but the different species of propositions; and Aldrich declares " hæc divisio peti dicitur a substantia propositionis;" the substance therefore of a proposition is the character of its assertion; i. e. whether the assertion be expressed absolutely or not absolutely, viz. conditionally; which are the only ways in which any assertion can be expressed; and in dividing propositions in this manner we must regard their whole essence, and not only the genus or material part of their essence; for sentences may be expressed in various ways, besides absolutely and conditionally: for instance, commands and questions are sentences, but are not propositions. Dr. Whately considers the substance as the genus or material part of the essence of propositions, and I consequently feel much diffidence in expressing an opinion which is at variance with an author who has treated the science of logic with such ability.
hypothesis: e. g. "I will walk if it does not rain ;" " You may either go or remain behind."

Division of categoricals.

The categorical proposition is divided into two kinds; viz. the pure categorical and the modal.

Pure.

Modal.

Division of hy potheticals.

The pure categorical proposition is that which asserts simply whether the subject does or does not agree with the predicate; as, "Nescit vox missa reverti ;" "George the Fourth is the king of England."

The modal categorical ${ }^{\text {h }}$ expresses in what mode or manner the subject does or does not agree with the predicate: as, "Such a fact may perhaps be true;" "No man can be perfectly righteous."

The only class of propositions which will be treated of at present will be the pure categorical.

The hypothetical proposition is divided into either conditional, as, " Riches, if badly applied, are a curse, and not a blessing;" or disjunctive;

[^23]as, " Pleasure should either be taken in moderation, or not at all." "This result is the effect either of truth, which produces consistency without the writer's thought or care, or of a contexture of forgeries confirming and falling in with one another by a species of fortuity, of which I know no example." Horæ Paulinæ, c. viii. §. 4.

Another division of propositions is by regard- Quality. ing their quality, and of quality there may be two sorts; viz. the quality of the expression, or oftwokinds, the essential quality; which is the differentia; accidinatal. and the quality of the matter, or the accidental quality; which is consequently the property.

Propositions are divided according to their essential quality, into affrmative and negative ${ }^{\text {i }}$.

[^24]Affirmative propositions.

An affrmatied proposition is that which asserts that its extremes agree with each other; i. e. that the predicate may be asserted of the subject; as, " Oxford is a city containing an university;" "An Englishman will fight in defence of his country."

Negative propositions.

A negative proposition is that which asserts that its extremes disagree ; i. e. that the predicate cannot be asserted of the subject: as, "No Christian fears the hour of death;" "Nemo mortalium omnibus horis sapit."

Propositions are also divided according to their accidental quality, or quality of the matter, into true and false: and this is said to be the property, inasmuch as it results ${ }^{k}$ from the essence of the proposition; i. e. from the difference or assertion, which must of necessity be either true or false.

A true proposition is that which asserts what is the real fact; as, "The object of logic is to
$k$ The necessary consequence which results from any assertion is, that it must be either true or false, which is the accidental quality, or qualitas rei, as it is commonly termed : to ascertain the truth or falsehood of any proposition is not the office of logic: but it must be proved by a consideration of that science or art to which the subject-matter of the proposition belongs : consequently, as will be shown hereafter, the truth or falsehood of every proposition will depend upon its matter, viz. the connexion which naturally exists between its extremes. N. B. When we speak of the quality of a proposition, without declaring which kind, the essential quality, or qualitas vocis, is meant ; viz. its being affirmative or negative.
direct the mind in the acquisition of knowledge:"
" England is an island."
A false proposition is that which asserts what Palte propois not the fact: as, " Logic is the art of using the reason;" "A murderer is not deserving of punishment."

Propositions may also be divided, by regarding their quartity, into universal, particular, singular, and indefinite.

The quantity of a proposition means " the Quantity. extent" to which the predicate is asserted of the subject.
An universal proposition is when the predicate Univeral is asserted of the whole of theosition. is asserted of the whole of the subject; and since the subject is in this case taken in its whole sense, i. e. " for every thing signified by it;" it is said to be distributed ${ }^{1}$; and this distribution is indicated by some sign of universality, as " all," " none," " every one," \&c.; e.g. " All bad passions are to be avoided;" "No virtuous act will lose its reward."
A particular proposition is that whose predi- $\underset{\substack{\text { Praricular } \\ \text { propoitions. }}}{\text {. }}$

[^25]cate is asserted of only a part of the subject; and since, in this case, the subject is not taken for every thing signified by it, hence it is not distributed: and this is indicated by a sign of particularity prefixed to it, as "some," "few," " many," \&c.; e. g. " Some men are possessed of more judgement than others;" "Not every one that saith unto me, Lord, Lord, shall enter into the kingdom of heaven."

Singular propositions.

A singular proposition is that whose subject is a singular noun; or a common noun with a singular sign : [see Part I. Sect. III.] e. g. "Dionysius was a tyrant;" "That man is a thief;" but since in all cases of singular propositions the predicate is asserted of the whole of the subject, hence the subject is distributed; and singular propositions are [see the next section] consideręd as universals.

With respect to indefinite propositions ${ }^{m}$, they are such as have common terms for their subjects,
m Any proposition (except a singular) to whose subject there is not affixed some sign, denoting whether that common noun is to be taken for everything signified by it, or not, must be regarded as indefnite ; because the extent in which that subject is taken is not limited; but in order to ascertain this extent, we must apply to our common sense, and also to a knowledge of that particular science or art to which the proposition relates: in other words, we must look to the matter, and by that we must be guided: but indefinites need not be classed as a distinct species of propositions; because they must be either universals or particulars, since the predicate must be said either of the whole or only of a part of the subject.
but they have not any sign, either of universality or particularity, whereby we may know whether the subject is to be taken in its fullest sense or not; but inasmuch as it is evident that the predicate must be asserted either universally or partially of the subject, it is obvious that all indefinite propositions may be classed under universals or particulars, according as their predicate is said of the whole or only a part of the subject; and this must be ascertained from the natural connexion existing between the subject and the predicate, which is called the matter of the proposition; and which will be explained in the next section. It is useless therefore to consider indefinites as a separate class of propositions. Thus it appears that, strictly speaking, propositions, divided by considering their quantity, are of two kinds, viz. universal and particular.

In order to keep this in mind, the following line was formed:

Quse $\}$ Ca. vel Hyp. Qualis $\}$ Ne. vel Aff. Quanta ? Uni. Par. Ind. Sing.n
n The words of this line, when written at full length, are as follows: "Quæ? Categorica vel hypothetica. Qualis? 'Negativa vel affirmativa. Quanta? Universalis, particularis, indefinita, singularis." The meaning of it may be thus explained: Propositions divided as to substance, (Quæ ?) are categorical or hypothetical: as to quality, (Qualis?) they are negative or affirmative: as to quantity, (Quanta?) they are either universal, particular, indefinite, or singular.
The following Table presents at one view the division of Propositions, with their subdivisions.


## SECTION III.

In every singular proposition, the predicate is said of the whole of the subject, i. e. the subject is taken for every thing signified by it, or is distributed; e. g. "Dionysius was a tyrant:" here the whole of Dionysius is meant; consequently, in a syllogism, singular propositions are considered as equivalent to universals ${ }^{\circ}$.

The matter of a proposition is the " extent of Matter. connexion which naturally exists between the extremes;" and it is of three kinds, necessary, impossible, and contingent.

Necessary matter is when the extremes of a Necesary. proposition essentially and invariably agree with each other, as, "All islands are surrounded by water."

[^26]$$
\text { D } 3
$$

Impossible.

## Contingent.

Indefinites.

Impossible matter is when the extremes of a proposition differ from each other essentially and invariably, as, " No human institution is wholly without error."

Contingent matter is when the extremes of a proposition partly agree with each other, and partly differ, as, "Some human inventions are beneficial to mankind."

The quantity of indefinite propositions may be determined by these different kinds of matter ; for in necessary and impossible matter, an indefinite may be considered as an universal, and the sign of universality may be prefixed; e.g. " Human inventions are liable to error;" in which case we may say, " All human inventions," \&c. and, "Honourable men are not willing to disgrace their characters;" that is, "No honourable men," \&c.; but in contingent matter, i. e. when the extremes only partially agree, an indefinite proposition must be considered as a particular; e. g. " Victories have been more destructive to the conquerors than to the conquered;" that is, "Some victories," \&c.; and, " Works of human invention are steam engines;" that is, "Some works," \&c.

Four classes of propositions.

Pure categorical propositions ${ }^{\mathrm{p}}$ being regarded according to their quality and quantity, may be

[^27]considered as of four kinds, viz. "universal affirmative," " universal negative," " particular affirmative," and "particular negative." And each of these classes is denoted by a particular symbol; thus, A stands for the universal affirmative, E the universal negative, I the particular affirmative, and $O$ the particular negative, which is expressed in the two following verses:
^sserit A, negat E; universaliter ambe;
Asserit I, negat O; sed particulariter ambo.
Since in every universal proposition the pre- Distribution dicate is said of the whole of the subject, hence the subject is distributed in every universal ${ }^{9}$ :
many classes propositions may be considered to be, as far as may serve for syllogistic reasoning. With respect to substance, we shall consider only one class, viz. pure categoricals: and by regarding the quality (viz. the essential quality) and the quantity, it has been shown that there are two classes of each; i. e. affirmative and negative, universal and particular; hence it is manifest that there cannot be more than these four classes: universal affirmative, universal negative, particular affirmative, and particular negative.
9 With respect to the subject of an universal proposition being distributed, it is self-evident that this is the case, it being the differentia of an universal proposition : the fact is equally clear with respect to the distribution of the predicate in the universal negative: but in the particular negative it is not so manifest that this is the case: it may, however, be proved thus, "Some men are not logicians." This proposition asserts, that there is a certain class of men, no one of which is a logician, viz. there is some limited number of individuals comprised in the subject, fron which every individual comprehended under the predicate is wholly excluded: or, in other words, the term logician, in its
but in negative propositions, the predicate must be distributed, or the proposition could not be true: thus, " No human institution is perfect," would be false, if any part even of the term " perfect" agreed with the term "human institution." The distribution, therefore, of the terms of propositions depends upon their universality and their negation; hence this rule may be formed,
General role. "All universals distribute the sulject, and all negatives distribute the predicate."

Predicate of an aftirmative sometimes distributed.

It sometimes happens that the predicate of an affirmative is distributed ${ }^{\mathrm{r}}$; but since this circum-
most extensive signification, cannot be predicated of any individual comprised under that class of men, which is the subject; consequently it is evident that the term logician is here used in its most universal sense, viz. it is distributed; and unless it were so distributed, the proposition, "Some men are not logicians," would not be true.
r The predicate of an affirmative proposition cannot, with accuracy, be ever said to be distributed; for although it may accidentally happen that the predicate be of equal extent with the subject, i. e. that the predicate in its fullest sense may be affirmed of the subject, also distributed, yet this fact is by no means implied in the form of expression of the affirmative proposition : the predicate, therefore, is not " actually distributed," (Whately)" but is distributable; and the point to be considered is, not what might be said with truth, but what actually has been said." A case somewhat similar to the present occurs in the reduction of one of the modes of syllogisms in Part III. which will be shown hereafter. It often happens that the predicate is of equal extent with the subject of an affirmative proposition, and is therefore distributable, as is the case in most mathematical definitions; e. g. a " rectilineal triangle is a plane figure

## ON THE OPPOSITION OF PROPOSITIONS.

stance does not depend upon the form of the expression, but is merely accidental, resulting (as Aldrich observes, chap. ii. § 3.) " virtute significati, non virtute signi;" it is not to be considered so as to affect any argument; nor could any inference be drawn which depended on such a circumstance; for the form of the expression alone is regarded in logic, the truth or falsehood of a proposition depending upon its subject matter.

## SECTION IV.

Two propositions are said to be opposed to Opposition. each other, when, the subject and predicate being the same in each, they differ from each other either in quantity or in quality, or in both; and since there are four different classes of propositions which may be formed, each having the same subject and predicate, viz. A, E, I, and $O$; any two of which are said to be opposeds,
contained by three straight lines :" also in all metaphysical definitions, as, "A proposition is an asserting sentence;" or where the predicate is any specific property of the subject, as, "A proposition is a sentence signifying something true or false:" if, then, any conclusion be deduced from such a case as this, such a conclusion may materially be correct, but it must be inaccurate according to the rules of logic, because it could not be deduced from the form of the expression alone.

- Propositions, when opposed to each other, are said to have the same subject and predicate; and the points in which they
consequently there are four different kinds of opposition; i.e, contrary, subcontrary, subaltern, and contradictory.
Contrary.
Contrary opposition ${ }^{t}$ is between two universal propositions, differing from each other in quality only, viz. between A and E: e. g. "All men are mortal;" " No men are mortal."
Subcontrary. Subcontrary opposition is between two particular propositions, which differ from each other in quality only, viz. between I and O: e. g. "Some men are logicians;" "Some men are not logicians."
Subalteru.
Subaltern opposition is between two propositions which differ from each other in quan-
are to differ is in quality or in quantity, or in both; but it must be remembered, that when any propositions oppose each other, they are not only to have the same subject and predicate, but those terms are to be used with reference to each other in exactly the same sense in both the propositions, or no opposition can subsist between them. This rule, which Aldrich has stated as applying to contradictories alone, (see chap. ii. § 4.) is equally applicable to all the other species of opposition; and if this were not observed, the four kinds of propositions might be all true or all false together.
${ }^{\text {t }}$ The opposition which exists between two singular propositions can only be contrary opposition, for the quantity of singulars cannot be hanged, (except by conversion); but since the matter of a singular proposition cannot be contingent, hence the contrary to a singular forms as perfect an opposition as contradiction; for if a singular be true, its contrary must of necessity be false, and vice versâ; for it will be shown in this section, that contraries cannot be both true or both false together, either in necessary or impossible matter.
tity only; viz. between A and I, or between E and O :
e. g. $\left\{\begin{array}{l}\text { All human institutions are imperfect; }\end{array}\right.$ Some human institutions are imperfect.
or, $\left\{\begin{array}{l}\text { No equivocator is a person worthy of credit; } \\ \text { Some equivocator is not a person worthy of credit. }\end{array}\right.$
Contradictory opposition is between two pure contraliccategorical propositions, differing from each other both in quantity and quality, viz. between $A$ and O , or E and I:
e. g. $\{$ All virtues grace those who possess them;

Some virtues do not grace those who possess them.
or, $\left\{\begin{array}{l}\text { No sophistical argument is to be relied on; }\end{array}\right.$
Some sophistical argument is to be relied on.
N.B. In order that two propositions should be contradictories, (and such cannot be both true nor both false together,) care must be taken that the terms of both the propositions are to be used in exactly the same sense ${ }^{\text {u }}$ with respect to each other.


#### Abstract

aldrich has given this rule in the following words: "Notandum est, ad contradictionem requiri quatuor: nempe loqui de eodem, 1. eodem modo; 2. secundum idem; 3. ad idem; 4. in eodem tempore." (Vide chap. ii. § 4.) All of these requisites may be comprehended in this one general rule, viz. That the subject and predicate of the opposing propositions must be employed in exactly the same sense with respect to each other : and this rule applies (as has been shown above) to all the cases of opposition, as well as to the particular one of contradiction. Contradictories are perfectly opposed to each other, e. g. "All men are logicians;" "Some men are not logicians:" what the one proposition affirms universally, the other denies partially; again, " No men are dogs;" "Some men are dogs;" in this


Which kind of opposition is nost com. plete.

Of all these four kinds of opposition, the contradictory is the most perfect; for contradictories differ from each other in all points, viz. not only in quality, (the one being negative and the other affirmative,) but in quantity also, for the one is universal and the other particular ; therefore it is manifest, that when any proposition is true, its contradictory must of necessity be false; and, conversely, if any proposition be false, the contradictory to it must be true.

Truth and falsehood depend upon the matter.

Since in every proposition the assertion is respecting the relation which the extremes bear to each other, it is obvious that the truth or falsehood of that assertion must depend upon the relation which naturally does exist between those extremes, viz. upon the matter. The relation, which is expressed in a proposition, between its extremes, is that of their agreement or disagreement with each other: the rule, therefore, which may be formed with respect to the truth or falsehood of propositions in the different kinds of matter, is as follows: whenever the assertion of a proposition, respecting the mutual agreement or disagreement of its extremes, coincides with

[^28]what is known ${ }^{\times}$by the matter, respecting their real connexion, then the proposition is a true one, and vice versá thus, in necessary matter, it is known that the extremes invariably and essentially agree, consequently all affirmatives (which assert the agreement of their extremes) will be true: but negatives, which assert that they disagree, are of course false: the case is the same with respect to all the different kinds of matter. Hence the following rules will be self-evident:

| In necessary matter,, | Affirmatives, true. <br> Negatives, false. |
| ---: | :--- |
| In impossible matter, | Affirmatives, false. <br> Negatives, true. |
| In contingentmatter, | Universals, false. <br> Particulars, true. |

The following scheme presents at one view scheme of the different species of propositions, denoted ${ }^{\text {opposition. }}$ by their respective symbols, $A, E, I, O$; the different kinds of matter, by the initial letters n.i.c.; and the truth or falsehood of the pro-

[^29]positions in each matter by the letters $t$. and $f$. viz. true or false.


By an inspection of this scheme it will be manifest, that the contraries cannot be both true together, nor the subcontraries both false, with many other observations: and if the matter be known, the truth or falsehood of any proposition may be easily discovered.
General rale. N. B. (1.) If an universal be true ${ }^{\mathrm{y}}$, the particular contained under it will also be true: for

F Thus if it be true that " $A l l$ human institutions are liable to imperfection," it necessarily must be true that "Some human institutions are liable to imperfection." Again, if it be false
if the predicate may be asserted of the whole of the subject, of course it may be asserted of a part of $i$ it.
(2.) If a particular be false, the universal which contains it will be false also: for if the predicate cannot be asserted of a part of the subject, à fortiori it cannot be asserted of the whole of it; since the whole must contain that part.

If the universal be false ${ }^{2}$, or the particular true, the particular to the one and universal to the other may be either true or false; and unless the matter be known, it cannot be discovered which they are. It would be useless to go through all the various proofs which Aldrich has given to show that A and E cannot be true together, but may be both false; that
that "Some vicious habits are worthy of receiving commendation," it will evidently be false to predicate of all vicious habits, that they are worthy of receiving commendation : for as the predicate cannot be said of a part of the subject, of course it cannot of the whole of it, since the term, "Some vicious habits" is contained under " $A l l$ vicious habits."
" Let the universal be false, e.g. "All men are acquainted with the science of astronomy;" although the predicate cannot be asserted of the whole of the subject, it does not therefore follow that it may not be asserted of a part of it; as, "Some men are acquainted with the science of astronomy." In a similar manner it may be shown, that if the particular be true, it does not therefore necessarily follow that the universal must be so; for though the predicate may be asserted of a part of the subject, it does not necessarily follow that it may be asserted of the whole of it : the example just given will serve as an illustration.

I and O may be both true, but cannot be both false together, \&c.; for the conclusions are selfevident, and by a knowledge of the rules above given, relative to the truth or falsehood of propositions in the different kinds of matter, these deductions will be manifest.

## SECTION V.

Conversion. A proposition is said to be converted when its extremes are transposed.
ortwo kinds. There are two kinds of conversion ${ }^{\text {a }}$ generally used in logic, viz. simple conversion and conversion per accidens.
a There is also another kind of conversion, which is not mentioned by Aldrich, but which is of use in logic ; this is called conversion by contraposition: Dr. Whately calls it, conversion by negation : it is effected by changing the quality of the proposition, viz. in the case of 0 , you may conceive the negative as a part of the predicate; regarding the proposition as I, instead of $\mathbf{O}$; thus, though the terms are not strictly the same as before, yet the meaning of the proposition will not be altered: e.g. "Some men are not-logicians;" here we may consider the predicate as " not-logicians," instead of "logicians," and the proposition will stand thus:
" Some men are not-logicians;"
viz. " Some men are beings who are not-logicians."
And this proposition being I, may thus be simply converted;
"Some beings who are not-logicians are men."
By this mode A may be simply converted, when reduced to the form of E , by introducing a double negative in the place of the affirmation; the meaning of the proposition will not, of course, be altered by such a circumstance: "for," says Dr. Whately,

Simple conversion is the mere transposition of simple. the extremes of a proposition, without any change of the quantity or quality ; e. g. " No species of injustice is tolerable :" converted thus, "Nothing tolerable is a species of injustice." "Some works of art are of human invention," converted to " Some things of human invention are works of art.

Conversion per accidens, or (as Dr. Whately Per accidens more properly terms it) conversion by limitation, is when the extremes of the proposition are transposed, and the quantity is changed also ${ }^{\text {b }}$; e. g. "All quadrupeds are animals," converted to, " Some animals are quadrupeds." "No tyrant
" it is the same thing to affirm some attribute of the subject, or to deny the absence of that attribute," e.g.
" Every act of prudence is an act of virtue."
This is exactly equivalent to
" No act of prudence is not an act of virtue."
This being E, may consequently be simply converted; therefore "That which is not an act of virtue, is not an act of prudence;" or, "No act but a virtuous one can be an act of prudence:" i. e. " A virtuous act alone can be an act of prudence."
Thus by some one of the three modes of conversion, any proposition may be converted; viz. $\mathrm{E}, \mathrm{I}$ may be converted simply, E, A per accidens, and A, O by contraposition.

The following lines have been formed by logicians, in order to assist the mind in remembering these rules of conversion. F E c I simpliciter convertitur, E v A per acci. FAxO per contra: sic fit conversio tota.
b Accidental conversion depends upon the laws of subaltern opposition, in which it has before been shown, that if the universal be true, the particular will also be so; but if the universal be false, it does not necessarily follow that the particular must
deserves the love and esteem of his subjects," converted to, "Some person who deserves the love and esteem of his subjects is not a tyrant."
The truth of a proposition is not in any way affected by logical conversion; hence if a proposition be true before conversion, it must be so after, viz. its converse must also be true; for

Illative conversion.

Rule for illative conversion. " conversio utrobique illativa est ${ }^{\text {c.". Illative con- }}$ version is, when the truth of the converse follows from that of the proposition which has been converted, or exposita, as it is termed; and all conversion, as used in logic, must be illative.

Hence we may deduce the following general rule: viz. No term must be distributed after conversion which was not distributed before it; for in this case the term which was employed only partially in the exposita, has been used
be false: hence it is obvious, that if any universal be true, its accidental converse will also be true; but if false, the accidental converse may be true: e.g. if it be true that "No men are quadrupeds," it will also be true that "Some quadrupeds are not men ;" but if it be false, that ". No men are liable to death," it is not necessarily false that " Some beings liable to death are not men;" for this assertion is manifestly true. Hence it may be seen, that accidental conversion is not so complete an inference as simple conversion; for the simple converse of a proposition always follows the accidental quality of the exposita, viz. if the exposita be true or false, its simple converse is the same, (provided it be such a proposition as admits of being simply converted), but the accidental converse of a proposition does not follow the accidental quality of the exposita, unless the exposita be true.
${ }^{\text {c }}$ Aldrich, chap. ii. § 5.
universally in the converse: and it has been proved above, (see last section, p. 67.) that the truth of an universal cannot be inferred from that of its particular.

From a consideration of this rule it will appear, that A and E may be converted per accidens, and E and I simply; and such conversion will be in all cases illative.

The following memorial line was formed in Memorial order to keep this circumstance in the student's ${ }^{\text {line. }}$ remembrance:

F E C I simpliciter convertitur, E v A per acci.
viz. E and I are simply converted, E and A per accidens. In order that a proposition may be E and I concapable of being simply converted, it is necessary pert. that its extremes should be of equal extent; i. e. that either they should be both distributed, as is the case in the universal negative, or neither distributed, as in the particular affirmative ${ }^{\text {d }}$; for, let E be true; e.g. "No vice is commendable:" in this case both of the extremes differ essentially from each other; this proposition therefore denotes that vice differs from any commendable

[^30]thing; consequently, any thing that is commendable must differ from vice, or "No commendable thing is vice:" again, let I be true; e. g. "Some members of the university are good logicians." This proposition denotes the partial agreement of the two extremes; and since the terms good logicians, and members of the university agree, it follows that we can predicate of some good logicians, that they are members of the university: viz. "Some good logicians are members of the university;" or else the original proposition could not be true ${ }^{e}$.
A and E per
accidens. Let A be true, then I, its particular, must be true, and consequently the simple converse of I must be true; but this is the accidental converse of A: therefore A may be converted per accidens. That E may also be converted
$e$ Aldrich proves the simple converse of $I$ to be true in a different manner, (chap. ii. §5.) thus: if I be true, its contradictory (E) must be false; therefore the simple converse of that contradictory must also be false, consequently the contradictory to that simple converse must be true; but this is the simple converse of the original proposition (I) e.g.
I. "Some members of the university are good logicians:" (true.)
E. " No members of the university are good logicians:" (false.)
E. "No good logicians are members of the university:" (also false.)
therefore, (I) "Some good logicians are members of the university," must be true, and this is the simple converse of the original proposition, "Some members of the university are good logicians."
per accidens is self-evident; for since the simple converse of E is true, the particular contained under this converse, must be true also: but this. is the converse per accidens of the original proposition E .

O cannot be converted either simplyf or per 0 ont conaccidens; for since only one term is distributed, a term would necessarily be distributed after conversion, which was not so before.
f "As it was remarked that, in some affirmatives, the whole of the predicate does actually agree with the subject, so, when this is the case, and is granted to be so, A may be illatively converted simply; but this is an accidental circumstance."Elements of Logic.

On similar grounds it may be shown, that in impossible matter, 0 may be converted both simply and accidentally; for since the terms of the proposition must, by the matter, essentially and invariably differ, the universal which contains this particular must in such a case be true; and it has been shown, (see note b), that the simple and accidental converse of this proposition will both be true; and the simple and accidental converse of $\mathbf{E}$ will thus become the same as the accidental and simple converse of O: e.g. (let a case be taken in impossible matter;) let $O$ be true. "Some men are not dogs;" then by the matter, " No men are dogs," is true.
 But the former of these is the accidental converse, and the latter is the simple converse of the exposita; viz." Some men are not dogs." Let the case be proved generally thus: let it be assumed that the matter is impossible, then " Some A is not B," is true; but by the matter, " No $A$ is $B$," is true: hence " No B is A," and "Some B is not A," are also true. And these two last propositions are the accidental and simple converse of "Some A is not B."

## PART III. SECTION I.

Of argument. The third part of logic treats of argument or syllogism, which is the sign of the third mental operation; for discursus, or reasoning expressed in words, is argument.

Reasoning (or discourse) having been defined to be the progress of the mind from one or more judgements to another resulting from them, consequently every decomplex word which expresses reasoning, must consist of two parts ; that which is proved, and that by means of which it is proved. That by means of which any thing is

Connexion between the premises, proved is generally called the antecedent or premises ${ }^{\text {a }}$; and that which is proved is called the inference or conclusion.

The premises must have a connexion with each other; for if this were not the case, no conclusion could possibly result from them: e.g. " Jupiter was the king of the heathen gods;" " England is the mistress of the sea;" from two

[^31]such judgements nothing could be inferred, for there is no connexion existing between them, and they do not in any way depend upon each other: also there must be such a relation between the two premises and the conclusion, that, and between from a knowledge of the former, the mind must and conclus be irresistibly led to the latter.
Consequence, as employed in logic, is the conseqnence. mode of showing the dependence which exists between the antecedent and the consequent; i. e. between the premises and the conclusion: there are two kinds of consequance, the material and the formal.
The material consequence ${ }^{\mathrm{b}}$ is when the con- Material conscquence.

This reduction may seem unnecessary, because it may be urged, that under its other form the inference was sufficiently obvious; but yet it will be of advantage to reduce any material argument to a syllogistic form, because any error may then be more easily detected; for an argument which cannot be reduced to the above regular and logical form, cannot be legitimate. Just in the same way it is often of use to fill up the ellipses in a sentence, in order to see whether that sentence be grammatical.
sequent is inferred from the antecedent solely by the matter of the argument; i. e. by the force or meaning attached to the terms: e.g. "Diamonds are jewels; they are therefore valuable." "No brutes are human; consequently they are not rational." "Some pleasures are allowable, for they are innocent."

Formal consequence.

The formal consequence is when the consequent is inferred from the antecedent, from the form only of the expression; viz. from the disposition of the terms with respect to each other: e.g.
" All virtue is commendable;"
" Temperance is a virtue:"
therefore, "Temperance is commendable."
" All innocent things are allowable;"
" Some pleasures are innocent:"
therefore, " Some pleasures are allowable."
The formal consequence alone is regarded in logic ; for since it depends solely on the disposition of the terms with each other, it cannot ever fail; but the material, which depends only on the meaning of the terms, may frequently lead into error ${ }^{c}$.

[^32]A syllogism is an argument in which the terms syllogim. are so placed with respect to each other, that the conclusion results necessarily from the premises, from the mere force of the expression, and without any consideration of the meaning of the terms themselves.
Aldrich ${ }^{\text {d }}$ has defined a syllogism to be " oratio, in qua positis quibusdam atque concessis, necesse est aliud evenire, prater et proptere ea, qua posita sunt atque concessa." In a syllogism, the truth of the premises being admitted, it will be impossible to deny the conclusion : and even if the terms be changed, the inference will still hold good; e. g.
" All islands are surrounded by water;"
" England is an island:"
therefore, "England is surrounded by water."
The truth of this conclusion is so apparent, that it needs not a proof; for the mind, when once convinced of the truth of the two premises, cannot but admit that of the conclusion also; and this inference would be equally apparent, even if the terms were changed, and any symbols were
this circumstance will arise from the falsity of one of the premises, and not from the mode of inference; i. e. not from the force of expression, which alone is regarded in logic.
${ }^{4}$ See Aldrich, chap. iii. § 1.

- "Preter" means that the conclusion must be distinct from the premises, and the word "propter" signifies that the conclusion necessarily results by the force of those premises.
substituted in their place, provided that the arrangement of the terms be preserved; e. g.

Every B is A;<br>Every C is B:<br>therefore, Every $\mathbf{C}$ is A.

This inference is inevitable $f$, whatever terms be substituted for the letters A, B, C; and it is to this form that all real arguments may be ultimately reduced, and on their conformity or nonconformity to it their validity will invariably depend.

## SECTION II.

Of the simple categorical syllogism.

There are many kinds of syllogism; but, at present, the simple categorical will be the only one treated of: the simple categorical syllogism is that which consists of three pure categorical propositions : the two first of which are termed the premises, or antecedent, and the third is called the conclusion, or consequent ${ }^{\text {g }}$. The

[^33]conclusion, before it forms a part of the syllogism, and therefore has not been proved, is called the question or problem, because its truth is as yet uncertain: but after it has been proved, and forms a part of the syllogism, it is no longer uncertain, and is then termed the conclusion: e. g.

$\left.\begin{array}{c}\text { Question } \\ \text { or } \\ \text { Problem. }\end{array}\right\}$ " Is George the Fourth to be obeyed ?"
$\left.\begin{array}{c}\text { Antecedent } \\ \text { or } \\ \text { Premises. }\end{array}\right\}$ " All good kings are to be obeyed ;"
Conclusion. .." George the Fourth is to be obeyed."

The object of a syllogism is, to prove whether object of a the two extremes of the question agree or disagree with each other; and this cannot be done,
to the consequent by some causal conjunction, as, because, for, since, \&c.: e.g. "Blessed are the poor in spirit, for theirs is the kingdom of heaven." "The proof which arises from this perception is not to be deemed occult or imaginary, because it is incapable of being drawn out in words, or of being conveyed to the apprehension of the reader in any other way than by sending him to the books themselves." [Horæ Paulinæ, ch. xvi. 85.] This sentence may thus be reduced to a regular syllogistic form :
" A proof which is not capable of being drawn out in words, or of being conveyed to the apprehension of the reader in any other way than by sending him to the books themselves, is not to be deemed occult or imaginary;"
" The proof which arises from this perception is a proof of this kind :"

Therefore, "The proof which arises from this perception, is not to be deemed occult or imaginary."
but by comparing each of them with some one and the same third term. The following rules are those which are laid down in Aldrich's Logic ${ }^{\mathrm{h}}$ as the syllogistic canons; viz. those canons on which the whole force of syllogistic reasoning is founded. canons.

1. Quce conveniunt in uno aliquo eodemque tertio, ea conveniunt ${ }^{\text {i inter se. }}$
2. Quorum unum convenit, alterum differt uni et eidem tertio, ea differunt inter se: e. g.
"All men are liable to do wrong;"
(1.) "I am a man :"
therefore, " I am liable to do wrong."
Again :
" No science can be learned without application;"
(2.) " Logic is a science:"
therefore, " Logic cannot be learned without application."
3. Qua non conveniunt in uno aliquo eodemque tertio, ea non conveniunt inter se.

If there be two terms, such that no third term can be brought forward which may agree with both of them, they evidently cannot have any
${ }^{4}$ Chap. iii. § 2.
1 Two terms are said to agree with each other, when nothing exists in the one that does not also exist in the other, regard, of course, being paid to the extent in which the terms are used: the agreement or disagreement of terms, when expressed in logical propositions, is not contingent, but absolute : the different degrees of their agreement or disagreement not being regarded in syllogism: thus, "Some men are philosophers." Although both these terms are undistributed, yet their agreement is asserted absolutely in the proposition, and not contingently.
thing in common with each other; it will therefore be impossible to prove that they agree ${ }^{k}$.
4. Quorum neutri inest quod non sit in alio, ea non differunt inter se.
If there be any two terms which so exactly agree with each other, that there is not any idea comprised in the one which is not also comprised in the other, it will be impossible to prove that these two terms differ from each other; for manifestly no third term could be adduced with which one of these terms would agree, and from which the other could differ ${ }^{1}$.
5. Quce non probantur convenire in uno aliquo eodemque tertio, ea non probantur convenire inter se. Dubitari enim potest utrum detur ejusmodi tertium, et dubitatio ista non tollitur.
6. De quibus non probatur, convenire unum eidem alicui tertio, cui alterum differt, ea non probantur differre inter se. Dubitari enim potest, utrum detur ejusmodi tertium, h. e. utrum

[^34]alterutri insit quod non est in reliquo; et dubitatio ista non tollitur.

No two terms can be proved to agree or differ, unless by comparing them with some one and the same third term : if, therefore, no third term be adduced with which they are proved either both to agree, or one to agree with and the other to differ from, it is not proved whether they agree with or differ from each other: for since no third term has been used to compare them with, there remains a doubt whether any such term can possibly be adduced ${ }^{m}$; and until this doubt be removed, their agreement or disagreement with each other cannot possibly be inferred.

It is upon the two first of these rules that the validity of all simple categorical syllogisms depends: they may thus be rendered in English :
The twocbief 1. If any two terms agree with one and the canons. same third term, they agree with each other.
2. If of two terms one agrees with one and the

[^35]same third term from which the other differs, these two terms differ from each other.

It is upon the former of these that the validity of all affirmative conclusions depends, and on the latter, of all negative: of these rules Dr. Whately speaks thus: "No categorical syllogism can be faulty which does not violate these canons; none correct which does: hence on these two canons are built the rules or cautions which are to be observed with respect to syllogisms, for the purpose of ascertaining whether those canons have been strictly observed, or not."

## SECTION III.

Rule 1. In every syllogism there are three Thre terms terms, and three only. in a syllogism.
For every syllogism proves some conclusion, viz. proves the agreement or disagreement of two terms; and these two terms are not proved to agree or differ, unless by comparing them with some one and the same third term : the two terms, therefore, and the third, make three; hence no syllogism can have more than three terms. The following sentence, therefore, is not a syllogism:

[^36]In this apparent syllogism there are four terms ${ }^{\mathrm{n}}$; which are as follows: " Hector;" " the person who slew Patroclus;" "Achilles;" and " the person who slew Hector."

Major,minor and middle terms.

Three propo. sitions in a syllogism.
N.B. Of these three terms, the predicate of the conclusion is called the major term; and the subject of the conclusion is called the minor term; the third term, with which the major and minor terms are each separately compared, is called the middle : this term is called by Aristotle the argument. These names were assigned, because in an universal affirmative proposition, the predicate is commonly a more extensive term than the subject: whence arose the names of major and minor; so also the middle term is commonly in direct syllogisms (as will be seen hereafter) more extensive than the minor, but not so extensive as the major: whence it received the name of middle.
Rule 2. In every syllogism there are three propositions, and only three ${ }^{\circ}$.

[^37]For there are two premises in which the major and minor terms are each separately compared with the middle, and there is the conclusion, in which the major and minor terms are compared with each other: and the two premises with the conclusion make three propositions.
N. B. That premiss in which the major term is compared with the middle, is called the major premiss; and that in which the minor is compared with the middle, is called the minor premiss.
N. B. (1.) The major premiss is sometimes The propost termed "the proposition P ," and the minor is as ansomplion. called " the assumption."
only three comparative combinations can be made of three terms taken two and two together; viz. the major with the middle, the minor with the middle, and the minor with the major: and since no two terms can be compared but by a proposition, hence there cannot be more than three propositions in a syllogism.
p The major premiss is called "the proposition," by way of eminence, because when a syllogism is in its most perfect form, the major premiss is generally some well-known and universal principle which is not likely to be disputed; it is the minor premiss that is most liable to objection, because, generally speaking, it is an assertion, the truth of which is assumed, with particular reference to the question which is to be proved, hence the name " assumption;" e.g.
" All islands are surrounded by water;"
" England is an island:"
therefore, " England is surrounded by water."
In this example, the major premiss, "All islands are surrounded by water," is a well-known general truth; whereas "England is an island" is not a universal principle, as the major is, though accidentally it may be as well known; but yet,
(2.) The middle term must not enter the conclusion, for, in such a case, there would not be any inference drawn, since the two extremes of the question would not have been compared together : in fact, the last proposition would be but a conversion of one of the others; e.g.

> " No good logicians resort to sophistical arguments;"
> " All who are acquainted with the science of reasoning accurately are good logicians:"
> therefore, " None who resort to sophistical arguments are good logicians."

This is not a syllogism, for no inference is made; the conclusion being but the simple converse of the first proposition, the truth of which in no way depends upon that proposition which apparently is the minor premiss 9 .

Ambiguous middle.

Rule 3. The middle term must not be ambiguous.
The middle term being ambiguous, means that it must not be an equivocal term, which would admit of two meanings; for since in such a case the term would be employed in two dif-
in order to prove that "England is surrounded by water," it must be assumed that "it is an island."
q Aldrich observes, (chap. iii. § 3.), "Medium non ingreditur conclusionem, alias idem per idem probaretur ; adeoque non essent tres termini." I cannot see how the fact of the middle term being in the conclusion can affect the number of the terms, for surely in the two premises alone there are always three terms. There would be what is commonly termed " argumentum in circulo;" but would this have any influence on the number of the terms?
ferent senses in the premises, the extremes of the question would not be really compared with one and the same third term; there would, in fact, be two distinct middle terms, viz. there would be four terms ${ }^{r}$ employed: e.g.
" All spirits are inflammable;"
" A ghost is a spirit :"
therefore, " A ghost is inflammable."

The word " spirit" is here evidently used in a different sense in each proposition, consequently the two extremes of the conclusion are not compared with the same third term.

Rule 4. The middle term must be distributed:
For if the middle term be not distributed in midale not either of the premise the diatribated. either of the premises, the extremes of the conclusion will be compared with it, when employed only in a part of its signification; consequently,

[^38]since the two terms are each compared with $a$ part of the middle, there is no reason for knowing that they have been each compared with the same part ; hence one of the extremes may have been compared with one part of the middle, and the other with another part of it; e.g.

" Lead is a metal;"<br>" Gold is a metal :"<br>therefore, " Gold is lead."-Again :<br>" Some quadrupeds are winged;"<br>" A horse is a quadruped:"<br>therefore, " A horse is winged."

In these examples the middle term is not distributed, and there are therefore, in reality, four terms.

One distribution of the middle is safficient.

Rule 5. If the middle term be once distributed, it will be sufficient.

For if one extreme has been compared with the whole of the middle, and the other with a part of it, they will, in reality, have been compared with the same term ${ }^{\text {s }}$; e.g.

[^39]" All valuable knowledge is worth obtaining;"
" A correct knowledge of logic is valuable knowledge :" therefore, " A correct knowledge of logic is worth obtaining."

In this case, since one of the extremes agrees with the whole of the middle, and the other with a part of it, they both must entirely agree with that part of the middle; and they therefore do, in reality, both agree with one and the same third term ${ }^{\text {t }}$.

Rule 6. A term must not be distributed in the conclusion which has not been distributed in the premises.

This is termed an illicit process of the major $\begin{array}{r}\text { Illicit pra } \\ \text { cew. }\end{array}$
Now if it be granted, that the two extremes, " metals," and "lead," are compared to the third term " fusible," and to the same part of it, then this consequence may be materially inferred; but this cannot be proved, unless the middle be once taken in its most extensive sense, in which case it will be manifest, that the same part will have been compared with both of the extremes, and this part of the middle may be considered as one single term, with which both the extremes have been compared; the case is similar where one extreme agrees with the same part of the middle from which the other differs; e. g.
" Some men are not sophists;"
" Some men are good logicians:"
therefore, " Some good logicians are not sophists."
In this case the inference will be materially true, if it be admitted that the same class of men is meant in both premises; but, as before, this cannot be proved, unless the middle term be once distributed: hence the above arguments are incorrect in form, though true in sense, i. e. materially.
: In all perfect arguments, the middle term ought not to be more than once distributed; this will appear more evidently hereafter.
or minor term : and to employ a term universally in the conclusion, which was only partially employed in the premiss, must, of course, be erroneous; for the universal cannot be inferred from the particular: in fact, (as Dr. Whately observes,) there would be four terms; e.g.
> " Every virtuous act is worthy of commendation;"
> " Profane swearing is not a virtuous act:" therefore, " Profane swearing is not worthy of commendation."

> This conclusion could not be inferred from such premises, for the major term is illicitly distributed; and though the proposition may be true, yet its truth cannot be inferred from the premises: there are, in fact, two major terms ${ }^{\text {u }}$ instead of one; viz. "Some acts worthy of commendation," and " All acts worthy of commendation."

> Again :

" All countries surrounded by sea are insular;"
" Some barren lands are countries surrounded by sea:" therefore, " All barren lands are insular."

Here is an illicit process of the minor; the
a This rule, as well as the two preceding, may be considered as branches of the first; viz. that in every syllogism there must not be more than three terms : for an undistributed term and the same distributed, cannot be called one term : besides, to draw an inference from any term partially employed to the same term employed universally, is the same thing as inferring the universal from the truth of the particular, which is illicit, as has been shown above, (Part ii. § 4.), for a distributed term bears the same proportion to the same undistributed, as the universal to its particular.
argument is therefore false, for the same reasons as the preceding.

Rule 7. No inference can be drawn from Neative prenegative premises.

For in this case a middle term is brought forward, from which both extremes differ; and this fact does not afford any grounds for inferring that these two terms either agree with, or differ from each other ${ }^{\mathbf{x}}$; e. g.
" No real Christians are hateful to God;"
" A Mahometan is not a real Christian."
No conclusion can be drawn from such premises; the extremes may either agree or differ, but these premises will not prove their agreement or disagreement.

Rule 8. If one premiss be negative, the con- If one preclusion must be negative.

For since one premiss be negative, the other be negative. must (by the last rule) be affirmative; consequently one of the extremes agrees with the middle, and the other disagrees with it: hence it must be inferred that they differ from each other, and this disagreement cannot be expressed

[^40]but by negation; i.e. the conclusion must be negative ${ }^{\mathrm{y}}$; e. g.
" No species of injustice is tolerable;"
" An unjust law is a species of injustice:"
therefore, " An unjust law is not tolerable."

If the conclnsion be negative, one premiss mast be so.

Rule 9. If the conclusion be negative, one of the premises must be negative.

Since the conclusion is negative, the extremes differ from each other; consequently one of them must have differed from the middle, and this disagreement must have been expressed by a negative premiss ${ }^{2}$; e.g.
$y$ It should be remembered, that affirmative propositions assert the agreement, and negatives the disagreement, of their extremes: and since, in this case, one of the premises is negative and the other affirmative, one of the extremes is asserted to agree with the middle, and the other to differ from it; consequently it must be inferred that they differ from each, and this cannot be expressed but by a negative conclusion.
z It was before observed, (Part II. Sect. II.), that many propositions were apparently negative when they were not so ; this is the case when the negative does not really apply to the copula, but is, in fact, a part of one of the extremes : with such propositions a syllogism may seem to err against these three last rules, though in reality it will be correct; e.g.
"Those who are not dishonest deserve our esteem;"
" The virtuous man is not dishonest:"
therefore, "The virtuous man deserves our esteem."
Here one of the premises may seem to be negative; whereas they are, in fact, both affirmatives, and the syllogism is perfectly correct. Again,
" He who does not understand optics is not a complete mathematician ;"
" Many who read mathematics do not understand optics:" therefore, " Many who read mathematics are not complete mathematicians."
" No men of generous hearts remember injuries;"
" Englishmen are men of generous hearts:"
therefore, "Englishmen do not remember injuries."
Rule 10. No inference can be drawn from ${ }_{\text {Particnlar }}$ particular premises. premises.
For one of the premises must be negative, in order that the middle may be distributed; consequently the other premiss must (by Rule 7.) be affirmative: in these premises, therefore, only one term is distributed, which must be the middle : but since (owing to the negative premiss) the conclusion must be negative, the major term will be distributed in the conclusion, which was not distributed in the premises; consequently there will be an illicit process of the major ${ }^{\text {a }}$; e.g.

In this case, as before, the minor premiss appears to be negative, though in reality it is affirmative ; hence, in looking for negative premises, we must see whether the premises are really negative, or only apparently such; in which latter case they may be likely to lead into error.
a This rule, with respect to particular premises, is only a branch of some preceding ones: thus, if the premises were both particularly affirmative, they would err against the fourth rule, for the middle term would not be distributed; e.g. " Some arts are worth knowing:"
therefore, " Some arts are sciences."
Here the middle being undistributed, no conclusion can correctly be drawn. Again,
"Some men are not good logicians;"
" Some sophists are not good logicians."
From such premises no inference can be drawn (by Rule 7.), for they are both negative:-again, if these premises be taken,

> "Some brave men are not good officers;"
> " Some Englishmen are good officers:"
> therefore, " Some Englishmen are not brave men."

In this example there is an illicit process of the major term.
lfone premiss be particular, the conclusion must be so.

Rule 11. If one of the premises be particular, the conclusion must be particular.

The fault of drawing an universal conclusion, when one of the premises is particular, will be an illicit process of the minor term, as will be evident from the three following examples ${ }^{\text {b }}$ :

" All useful learning is praiseworthy ;"<br>" Some poetry is not praiseworthy :"<br>therefore, " No poetry is useful learning."-A gain,

one negative and the other affirmative, there would be an illicit process of the major, as is shown in the text: hence, in all cases of particular premises, there must be a violation of either Rules 4, 6, or 7.
b Three classes of premises may be formed, of which one is particular, viz. AI, EI, and AO, (for EO cannot be correct by Rule.7.) In the first case, it is manifest, that only one term will be distributed, which must be the middle : hence no term must be distributed in the conclusion; therefore the conclusion must be particular affirmative. Again, in the second case (viz. EI) two terms are distributed, whereof one must be the middle; therefore one only must be distributed in the conclusion: but the conclusion must be negative, (because of the negative premiss), and, in order to distribute but one term, it must be particular negative. The last case (viz. AO) may be proved exactly in the same way as the second, and the conclusion in this case also must be a particular negative. This eleventh rule, therefore, is but a branch of the sixth : for if an universal conclusion be drawn from one particular premiss, there will be an illicit process of the minor.

> "All meteors are vapours ;"
> "Some luminous bodies are vapours :"
> therefore, "All luminous bodies are meteors."-Again,
> " No works of human invention are perfect ;"
> "Some machines are works of human invention :"
therefore, " No machines are perfect."
Rule 12. A particular conclusion may be a particular drawn from universal premises.
conclusion from universal premises.

Whenever an universal conclusion can be drawn from universal premises, it will of course be allowable to infer a particular; for the truth of the particular may be inferred from that of the universal: but it will not, in all cases, be possible to infer an universal conclusion from two universal premises, and in such a case the conclusion must be particular; e. g.
" No branch of useful knowledge is attainable without some labour;"
" Every branch of useful knowledge is worthy of being attained :"
therefore, " Something which is worthy of being attained is not attainable without some labour."

In this instance, if the conclusion were inferred universally, it is manifest that there would be an illicit process of the minor term ${ }^{\text {c }}$.

[^41]On the name- An universal conclusion should always be less moods. inferred from universal premises, provided it be possible, without an illicit process; for although the particular conclusion must be true, if the universal is, yet the truth of the particular does not immediately result from the force of the premises, but rather from the truth of the universal: hence such form of inference is inaccurate, though not false ${ }^{d}$.

The above twelve rules are comprised in the following four lines, in order to assist the memory:
" Distribuas medium; nec quartus terminus adsit :"
" Utraque nec præmissa negans, nec particularis :"
"Sectetur partem conclusio deteriorem:"
"Et non distribuat, nisi cum præmissa, negetve."e
It is obvious that the number of these rules may be very much lessened; e. g. the third,
d The following syllogisms are therefore inaccurate, though not strictly incorrect :
" All works of art are of human invention ;"
" All machines are works of art:"
therefore, " Some machines are of human invention."
Again: "All crocodiles are amphibious animals;"
" No horses are amphibious animals:"
therefore," Some horses are not crocodiles."
Again: "All virtuous acts are the deeds of good men ;"
" The deeds of good men are not wicked deeds:"
therefore, "Some wicked deeds are not virtuous acts."
In the above syllogisms the conclusion ought to be universally drawn; the particular conclusions are therefore inaccurate, though not faulty.

- See Aldrich, chap. iii. § 3.
fourth, fifth, and sixth, are contained under the first : so that these rules may all be comprised under the five following:

1. There must not be more than three terms in any syllogism. This rule includes Rules 1, $3,4,5,6,10$, and 11 .
2. In every syllogism there are but three propositions.
3. The premises must not be both negative.
4. If one premiss be negative, the conclusion must be so, and vice versá. This includes Rules 8 and 9.
5. A particular conclusion may be deduced from universal premises ${ }^{\text {f }}$.

## SECTION IV.

By the above-mentioned rules, it may be determined how many moods may be formed by means of the four propositions $\mathrm{A}, \mathrm{E}, \mathrm{I}, \mathrm{O}$, so as to be useful for syllogism.

I In examining a syllogism, in order to see whether it be correct or not, we must apply to these twelve rules, for no syllogism can, in form, be incorrect, which does not violate any one of these. The following order will perhaps be found to be the most convenient for applying them. (1.) Count the terms and propositions. (2.) Look to the distribution of the middle. (3.) Illicit processes. (4.) Apply the three rules concerning negatives, viz. Rules 7, 8, and 9. Lastly, see whether the conclusion is particular, when the universal might have been inferred according to Rule 12.

A mood is defined to be " legitima determinatio propositionum secundum quantitatem et qualitatem8." When the three propositions of a syllogism are designated in their proper order, according to their quantity and quality, this is declaring the mood of the syllogism; e.g.

" Every bad habit should be avoided ;"<br>" Nothing that should be avoided is commendable:" therefore, " No commendable thing is a bad habit."

This syllogism is said to be in the mood AEE.

The namber of moods.

As there are four propositions which are used in syllogism, viz. A, E, I, O, and as any three of these, when combined, form a mood, it may thus be proved, that the whole number of permutations, which can possibly be formed, will be sixty-four ${ }^{\text {h }}$ : for each of these four propositions may be used as a major premiss, and each of

E See Aldrich, chap. iii. § 4.
${ }^{h}$ This is nothing more than a mere arithmetical calculation; for the number of permutations which can be formed of any four things taken three and three together, is $4 \times 4 \times 4=64$. The following is a list of all the moods:

AAA*, AAE, AAI*, AAO. AEA, AEE*, AEI, AEO* AIA, AIE, AII*, AIO. AOA, AOE, AOI, AOO*.

EAA, EAE*, EAI, EAO*. EEA, EEE, EEI, EEO. EIA, EIE, EII, EIO*. EOA, EOE, EOI, EOO.

IAA, IAE, IAI*, IAO. IEA, IEE, IEI, IEO. IIA, IIE, III, IIO. IOA, IOE, IOI, IOO.

OAA, OAE, OAI, OAO*. OEA, OEE, OEI, OEO. OIA, OIE, OII, OIO. OOA, OOE, OOI, OOO. Those moods which do not violate any of the twelve rules, and which consequently are useful for syllogism, are marked with an asterisk.
these major premises will admit of four different minors, (viz. A, E, I, or O,) therefore there may be formed four times four, or sixteen pairs of premises: so also every pair of premises may have four different conclusions, (viz. A, E, I, or O,) therefore the number of moods which can possibly be formed from the four different propositions, will be four times sixteen, or sixty-four.

Of all these sixty-four moods, it is manifest How many that many, in fact the greater part, will err $\begin{aligned} & \text { nefeim for fiyl- } \\ & \text { log. }\end{aligned}$ against some one or more of the above-mentioned rules ${ }^{\text {i }}$; e. g. AAO, which errs against the ninth, and OOE, which violates the sixth, seventh, tenth, and eleventh; and by an examination of all the moods, it will be found that out of the sixty-four, there will remain but eleven which will be useful for syllogism, viz. AAA, AAI, AEE, AEO, AII, AOO, EAE, EAO, EIO, IAI, OAO. Aldrich has given IEO, as one of the moods,
${ }^{1}$ By Rule 7. Sixteen are excluded, for having both premises negative.

By Rule 8. Twelve are excluded, for having affrmative conclusions, with a negative premiss.

By Rule 9. Four are excluded, for having negative conclusions, without any negative premiss.
By Rule 10. Twelve are excluded, for having both premises particular.
By Rule 11. Eight are excluded, for having universal conclusions, with a particular premiss.
There is also one excluded by the sixth rule, for having an illicit process of the major term, viz. IEO. [See the end of this section.]
" ad syllogismum utiles ${ }^{k}$ :" " which can be used in a legitimate syllogism :" but this mood must be necessarily and essentially faulty, and never can be used in any legitimate syllogism; for the major term will be distributed in the negative conclusion, which was not distributed in the major premiss, which is a particular affirmative, and does not distribute any term ; consequently, with such a mood as IEO, there must in all cases be an illicit process of the major ${ }^{1}$.

## SECTION V.

The figure of a syllogism.

The figure of a syllogism depends upon the situation of the middle term, with reference to the extremes of the question; (i. e. the major and the minor terms.)
Four figures. There are only four figures; for since there are but three terms to be compared together in a syllogism, and the middle term is confined to

[^42]
## on the figures. <br> 101

the premises, it is manifest, that the middle could not be placed in more than four different situations with respect to the major and minor terms.

In the first figure, the middle term is the First igure. subject of the major premiss, and the predicate of the minor.

In the second figure, the middle term is the second predicate of both premises.

In the third figure, the middle term is the Third subject of both premises.

In the fourth figure, the middle term is the Poarth predicate of the major premiss, and the subject of the minor ${ }^{m}$.

It is to be remembered, that, of the premises, orrie of tie the major premiss ought properly to be placed first, and the minor second; for otherwise the
$m$ For the sake of illustrating the different positions of the middle term, with respect to the extremes, the following syllogism is given with its terms disposed according to all the figures.

> 1st Fig. "No sophists are logicians;"
> " Some men are sophists:"
> "Some men are not logicians."
> 2nd Fig. "No logicians are sophists;"
> " Some men are sophists:"
> " Some men are not logicians."
> 3rd Fig. "No sophists are logicians;"
> " Some sophists are men :"
> "Some men are not logicians."
> 4th Fig. "No logicians are sophists ;"
> "Some sophists are men:"
> "Some men are not logicians."
first figure might appear to be the fourth, and the fourth might be taken for the first. The major premiss is that in which the major term is compared with the middle, wherever it happens to be placed ; so the minor is that which contains the minor term, whether it comes first or second.

Scheme of the figures.

The following scheme presents, at one view, the four different figures; in which A represents the major term, $\mathbf{C}$ the minor, and $\mathbf{B}$ the middle:

| 1st Fig. | 2nd Fig. | 3rd Fig. | 4th Fig. |
| :---: | :---: | :---: | :---: |
| B, A. | A, B. | B, A. | A, B. |
| C, B. | C, B. | B, C. | B, C. |
| C, A. | C, A. | C, A. | C, A. |

In this scheme, the terms of the propositions are only denoted, without stating their quantity or quality ${ }^{\mathrm{n}}$.

Each figure contains six moods.

Of these figures, each contains six moods, which will not violate any of the twelve rules given above: it is obvious, therefore, that the same mood must be allowable in different figures; e. g. IAI, and AAI, in the third and fourth figures, and EAE, EIO, in the first and second, with many others, so also it may be found, by examination, that a mood, which will be allowable in one figure, will violate some rule if used

[^43]in another; thus AAA is allowable in the first figure, but if it were used in the third or fourth, the result would be an illicit process of the minor ${ }^{\circ}$. Although each figure admits of six Nameless moods, yet several of these are useless, inasmuch as their conclusions are particular, when the universal might have been inferred: e.g. EAO, in the first figure.
> " Nothing which belongs to man is perfect;"
> " Every art is that which belongs to man:"
> hence, " Some art is not perfect."

Here an universal conclusion might have been inferred; therefore the particular (though valid) is useless and inaccurate. Of these moods there are five in number, out of the twenty-four, which may be used in all the figures; for the nineteen, which remain, (excluding these five,) certain names have been formed by logicians, which serve to denote the mood and figure; for, as it was before observed, the same mood (without

- Thus, in the third figure :

> "All felons are thieves;"
> "All felons are amenable to the law :"
> therefore, " All who are amenable to the law are thieves."

Again, in the fourth figure :
" All thieves are felons;"
" All felons are amenable to the law:"
therefore, " All who are amenable to the law are thieves."
In both these examples, it will be seen that there is an illicit process of the minor term.
regarding the figure ${ }^{\mathrm{P}}$ ) is used in different figures, hence the vowels, which denote the mood, would not alone point out the figure. The following lines denote the moods which are used in the four figures, signified by their respective names:

Names of all the moods.
(Fig. 1.) BArbArA, CElArEnt, DArII, FErIO que prioris :
(Fig. 2.) CEsArE, CAmEstrEs, FEstInO, BArOkO, secundæ;
(Fig. 3.) Tertia DArAptI, DIsAmIs, DAtIsI, FElAptOn, BOkArdO, FErIsOn habet : quarta insuper addit,
(Fig. 4.) BrAmAntIp, CAmEnEs, DImArIs, FEsApO, FrEsIsOn.

In the above lines, the three vowels denote the mood; i. e. the propositions of which the syllogism consists: the other letters serve to show the figure, as well as being of other uses, as will be shown hereafter. The five ${ }^{9}$ moods, whose conclusions are particular, when they might have been universal, have not any names affixed to them; for, in a strict argument, they are not

[^44]$$
\text { ON REDUCTION. } 105
$$
considered as accurate, and they are certainly of no practical use.

## SECTION VI.

From the first and second of the syllogistic The first canons, it follows that these twenty-four moods clearet. are conclusive; but of all the four figures the first is the most evident; for it is the clearest and most natural, and to it Aristotle's "Dictum de Omni et Nullo," is immediately applicable.

The axiom which the schoolmen term the The Dictum "Dictum de Omni et Nullo," is that test which Nallo. may ultimately be applied to all legitimate arguments; and by their conformity or non-conformity to it, their validity will in all cases depend. It is thus explained by Aldrich ${ }^{\mathrm{r}}$. "Quod pradicatur universaliter de alio, (i. e. de termino distributo,) sive affirmative, sive negative, pradicatur similiter de omnibus sub eo contentis;" viz. "That which is predicated of a term distributed, whether affirmatively or negatively, may, in like manner, be predicatcd of every thing contained under it. There needs $A_{n}$ axion. no proof to establish the truth of this rule, for it is self-evident, and may therefore be justly termed an axiom.

$$
\begin{aligned}
& \text { ₹ Chap. iii. §. 6, } \\
& \text { F } 3
\end{aligned}
$$

The four moods of the first figure, viz. Barbara, Celarent, Darii, and Ferio, are, under their present form, immediately applicable to this dictum; e.g. " A good king should be obeyed by his subjects ;"
" George the Fourth is a good king :"
therefore, " George the Fourth should be obeyed by his subjects."

In this syllogism', the major term is predicated of the middle distributed, consequently (by the above axiom) the major can be predicated of any term which the middle contains; (i.e. of which the middle can be predicated;) but in the minor premiss, the middle term is predicated of the minor, consequently the major may be predicated of the minor: thus the dictum of Aristotle is immediately applicable to all the four moods of the first figure; and this circumstance depends solely on the position of the middle term, with respect to the major and minor; in other words, upon the figure, whence the moods of this figure

The perfect moods. were termed by Aristotle, " the perfect moods;"

[^45]because they do not require any change in order to make their conclusions more evident ${ }^{t}$ : the schoolmen called them, "the direct moods;" because their conclusions can be directly inferred from the premises.

The moods of the second, third, and fourth figures, are, (owing to the position of the middle term,) not so evident as those of the first; for Aristotle's dictum cannot be immediately applied; though ultimately this may be effected; and when this is done, the syllogism is said to be reduced, i. e. brought into the form of the first figure. It is on this account that these moods were termed " imperfect" and "indirect;" for the dictum The imper. . cannot be immediately applied to them without their undergoing some change in the order of their terms; i.e. without arranging those terms in such a manner that the moods, instead of being in the second, third, or fourth figures, are changed into the first; and when this is effected, these moods are said to be " perfici," " revocare," or "reduci"."

Reduction may therefore be defined," the Redacion. changing of any imperfect mood, and bringing it into the more perfect form of the first figure:" so

[^46]that the necessity of the inference may become more apparent.
Of two kinds. There are two kinds of reduction; viz. ostensive reduction, and reductio ad impossibile.

Oatensive reduction.

Ostensive reduction is the direct mode ${ }^{\mathrm{x}}$ of proof; viz. it shows that the conclusion is true, by changing the order of the terms of the reduced syllogism, and drawing from either the same conclusion as before, or the converse of it.

It is obvious that in ostensively reducing a syllogism we must not introduce any terms different from those in the reduced syllogism, nor any new proposition: all that we have granted to us is, that the premises of the syllogism, which we wish to reduce, are true; hence we may, of

[^47]course, transpose them, or convert them illatively; (for if any proposition be granted true, it is allowable [see Part II. Sect. V.] to infer the truth of its converse:) and it is by making use of this liberty, when necessary, that all imperfect syllogisms may be ostensively reducedy. It was principally for this purpose that the names were invented to all the different moods; and in each moodi. of those names it must be remembered, that the three vowels denote (as was before remarked) the mood: the initial consonants, viz. B, C, D, F, show to what mood in the first figure the syllogism is to be reduced; i.e. that mood whose initial consonant is the same. The letters $\mathbf{S}$ and $\mathbf{P}$ denote that those propositions to which

[^48]they are affixed must be converted either simply $(\mathrm{S})$ or per accidens $(\mathrm{P})$ : M denotes that the premises must be transposed, and $K$ shows that the syllogism must be reduced by reductio ad impossibile, which will be explained hereafter.
Examples of These rules being borne in mind, the reduction reduction. of a syllogism is a mere mechanical operation ${ }^{2}$; e. g.

CAm" Every man of sense is anxious to gain useful information;"
Es "No idle man is anxious to gain useful information :" trEs " No idle man is a man of sense."
In this syllogism, $m$ shows that we must transpose the premises, and $s$ denotes the simple conversion of both the minor premiss and the conclusion; and if these things be done, the syllogism will be found to be in the first figure, and in the mood Celarent, as the letter $e$ in Camestres denotes ${ }^{\text {a }}$.

[^49]CE "No person who is anxious to gain useful information is an idle man;"
$1 A$ "Every man of sense is anxious to gain useful information:"
rEnt " No man of sense is an idle man."
Again, Disamis may be reduced to Darii, thus:
DIs "Some musicians are mad;"
Am "All musicians are men :"
Is "Some men are mad."
DA " All musicians are men;"
rI "Some mad beings are musicians:"
I "Some mad beings are men."
In these two examples, the simple converse of the original conclusion is shown to be true by applying it to the dictum of Aristotle, viz. by reducing the original syllogism to the first figure; and since the converse of its conclusion is shown to be true, the truth of the original conclusion itself may be implied ${ }^{\text {b }}$.

In order to prove this conclusion true, it will be necessary to convert the minor premiss simply, thus :
" No Mahometans are Christians;"
"Some men of good understanding are Mahometans:" therefore, "Some men of good understanding are not Christians."

This syllogism, which is in the first figure, viz. Ferio, may be immediately applied to the " dictum de omni et nullo," and its conclusion is therefore correctly inferred; but the simple converse of the minor was implied (though not expressed) in the original syllogism.
b Again, Camenes may be reduced to Celarent, by transposing the premises, and simply converting the conclusion, thus, e.g.
/" All useful arts are worth learning ;"
" Nothing that is worth learning is of no value:"
therefore, "That which is of no value is not a useful art." reduced thus to Celarent:

Reductio ad impossibile.

The process of reductio ad impossibile is as follows: in the two moods, to which it is usually applied, (viz. Baroko and Bokardo,) substitute the contradictory of the conclusion for the particular negative premiss: and from the two universal affirmative premises thus formed, draw a conclusion in Barbara. This conclusion will be false, because it will contradict a premiss which was hypothetically true, consequently it may be inferred that the contradictory of the original conclusion must be false, and therefore the conclusion itself must have been true: this will be more fully treated of in the next section.

## SECTION VII.

The validity of ostensive reduction is manifest;

Validity of ostensive reduction. for the premises of the syllogism being hypothetically true, they must be equally true when either transposed or illatively converted ${ }^{\text {c }}$; and
" Nothing that is worth learning is of no value;"
" All useful arts are worth learning:"
therefore, " No useful arts are of no value."
And, note, that whenever the premises of any syllogism are transposed in its reduction, the conclusion must necessarily be converted; for since the major premiss is made the minor, so also the major term must be made the minor.

- In order to reduce Bramantip ostensively it is necessary to convert the conclusion accidentally, e.g.
" All true patriots have their country's welfare at heart;"
"All who have their country's welfare at heart are friends to religion :"
therefore, " Some friends to religion are true patriots."
the conclusion of the syllogism, when reduced, is either the same as the original one, or is only
This syllogism, which is Bramantip, may thus be reduced to Barbara:
" All who have their country's welfare at heart are friends to religion;"
" All true patriots have their country's welfare at heart :" therefore, "All true patriots are friends to religion."

The reason why in this mood the conclusion (I) may be accidentally converted is, that the major term has been distributed in the major premiss, and therefore is distributable in the conclusion : although, owing to the figure, it cannot be distributed. It has been laid down, (in Rule 6, Sect. III. of this Part,) that "a term must not be distributed in the conclusion, if it has not been distributed in its premiss;" and it should be remembered also, that " a term ought not to be undistributed in the conclusion, if it has been distributed in its premiss:" not that there will be any incorrectness in the syllogism, if the term be undistributed in the conclusion; but such a mode of argument is very inaccurate and unscientific; for (in the case of Bramantip) more is assumed with respect to the major term in the premises than can possibly be inferred in the conclusion; consequently this mood is the worst of all the moods, it being the only one in which this inaccuracy occurs. It may be observed, that when, from accidental circumstances, it is known that the predicate of $I$ is distributable, it follows that the matter of the proposition must be necessary : hence, in all such cases, I may be converted both simply and per accidens; and such conversion will, under these circumstances, be illative. In the same manner it has been shown ( p . 73, note f , ) that in impossible matter, 0 may be converted both simply and per accidens. It must not, however, be supposed that the conclusion, which is drawn from two universal affirmative propositions, will in all cases be in necessary matter, because it is so in Bramantip; for in Darapti the matter of the conclusion is generally contingent, though in Bramantip it is invariably necessary; but this depends, as was shown before, on the distribution of the major term in its premiss, and not because both the premises are universal affirmative. ,
its illative converse; and in the latter case it is obvious that the truth of the original conclusion may be inferred from the truth of its converse, which is the conclusion of the syllogism when reduced: hence this reduction is termed "ostensive," because it shows directly that the original conclusion is true; e.g.

$$
\begin{aligned}
& \text { CA "All men are liable to err ;" } \\
& \mathrm{mE} \text { "No being who is liable to err is perfect:" } \\
& \mathrm{nEs} \text { "No perfect being is a man." }
\end{aligned}
$$

This. syllogism, which is in the fourth figure, may be reduced to the first, by transposing the premises, and simply converting the conclusion, thus:

$$
\begin{aligned}
& \text { CE " No being who is liable to err is perfect;" } \\
& \text { 1A "All men are liable to err:" } \\
& \text { rEnt " No man is perfect." }
\end{aligned}
$$

In the first figure, the simple converse of the original conclusion is shown to be true; hence it may be inferred that the original conclusion itself must likewise be true.

Of reductio ad impossibile.

Reductio ad impossibile is the indirect mode of proof; which is, to admit the falsity of a conclusion, and show that by arguing from such falsity, an absurdity or impossibility will result: this mode of reduction is not usually applied to any moods, except Baroko and Bokardo, but it must not therefore be supposed that it is not equally applicable to any others; for, in fact, all
moods may be reduced by reductio ad impossibile, as well as ostensively ${ }^{\text {d }}$.
${ }^{d}$ Since there are two modes of reduction, viz, ostensive and ad impossibile, and as it has been shown that every mood may be reduced by ostensive reduction, it may not perhaps be uninteresting to observe, how the reductio ad impossibile may also be applied to all the moods, although it is generally employed for Baroko and Bokardo only : the process of reductio ad impossibile is to assume the conclusion to be false, and then trace the consequence of this assumption; which will, in all cases, be some palpable absurdity. Thus let a case be taken in Ferison :
"No men of bad principles are to be trusted;"
"Some men of bad principles are pleasant companions:" therefore, "Some pleasant companions are not to be trusted."
This syllogism may thus be reduced to Darii, by employing reductio ad impossibile : therefore, " Some men of bad principles are to be trusted."
In this reduction the conclusion was assumed to be false, and its contradictory was therefore assumed to be true; and from this contradictory, united to the original minor premiss, a new conclusion was drawn in Darii : this conclusion is manifestly false, because it contradicts the original major premiss, consequently (as is the case in Baroko or Bokardo) it must necessaquently (as is the case in Baroko or Bokardo) it must necessa-
rily follow that the contradictory of the original conclusion (which was assumed true) is in reality false; hence the original conclusion itself must be true.

If reductio ad impossibile be employed for all the different moods, it will be found that in this manner all their conclusions may be shown to be true; for the new conclusion will either contradict an original premiss, or else some proposition, the truth of which is deducible from that premiss; such as the particular contained by it, or its simple or accidental converse; thus in Fesapo,
" No unjust act is commendable;"
" Every commendable act deserves reward:"
therefore, "Some act deserving of reward is not an unjust act."

> " All pleasant companions are to be trusted;"
> "Some men of bad principles are pleasant companions:"

All moods may be thus reduced.

It valdity. The validity of reductio ad impossibile may be shown thus: Every conclusion must be either true or false : let it be assumed to be false, then its contradictory must be true; let, therefore, its contradictory be taken as a new premiss, and to it let one of the original premises be joined; place these premises in such a manner that the middle term may stand as in the first figure; then draw the conclusion from them: and it will be found that this new conclusion will contradict an original premiss ${ }^{e}$, which was granted true;

It may be shown that this conclusion cannot be false, by reducing it to Barbara, thus:
" Every act deserving of reward is an unjust act;"
" Every commendable act deserves reward :"
therefore, " Every commendable act is an unjust act."
This conclusion contradicts the accidental converse of the original major premiss, and must therefore be false; for since the major premiss is hypothetically true, hence it follows, by the laws of conversion, that its accidental converse must also be true, therefore the contradictory of this accidental converse must be false : from this fact, it may, as before, be inferred that the original conclusion cannot be false, i. e. it must be true.

By adopting some measures similar to the above, it may be shown that every mood may be reduced by reductio ad impossibile; and although this is of no practical use, yet it may be beneficial to the student in logic to practise himself in employing this kind of reduction to the different moods, whereby he will make himself perfectly acquainted with the different figures, and the manner of proving a conclusion true, by reducing it to the first figure, at the same time applying the rules of contradictory opposition.

- In the two moods, Baroko and Bokardo, for which reductio ad impossibile is usually employed, the new conclusion contradicts an original premiss, but if this reduction be used for
consequently the new conclusion must be false; now, as the form of the argument is correct, the error must lie in one of the premises; and it is manifest which one of the premises it must be, for one of them is an original one, which was hypothetically true, therefore the new premiss, which was assumed to be true, must, in reality, be false; viz. the contradictory of the original conclusion has been proved to be false, therefore the original conclusion itself must be true; e. g.

$$
\begin{aligned}
& \text { BAr " Every wise man is contented;" } \\
& \text { Ok "Some men are not contented:" } \\
& \text { O "Some men are not wise." }
\end{aligned}
$$

This syllogism may thus be reduced to Barbara :

> " Every wise man is contented;" (granted true.)
> " Every man is wise:" (assumed true.)
therefore, " Every man is contented."
This conclusion is manifestly false, because it is the contradictory of the original minor ${ }^{f}$
any of the other moods, it will be found, as was observed in the last note, that the new conclusion will not always contradict an original premiss, but sometimes a proposition, the truth of which is deducible from an original premiss; such as the particular contained under it, or its simple or accidental converse; which will be equally efficacious towards proving that the original conclusion cannot be false.
' In the two moods, Baroko and Bokardo, the contradictory of the conclusion must be substituted for the particular negative premiss, keeping the universal premiss in its original situation; with respect to the other moods which may be reduced by this mode, the contradictory of the conclusion must be made the
premiss; (which is hypothetically true;) and since the form is correct, one of the premises must be false: this cannot be the major, for it was granted true in the original syllogism ; therefore the minor premiss, viz. "Every man is wise," (which was assumed to be true,) must in reality be false; consequently the contradictory to this minor premiss must be true; but the contradictory to

> " Every man is wise," is,
> " Some men are not wise:"
and this is the original conclusion, which has thus been proved to be true ${ }^{5}$.
major or minor premiss, according as may be necessary for forming the syllogism in the first figure; by referring, however, to the memorial lines given in note d, p. 115, no mistake can possibly arise from this circumstance; for the contradictory of the conclusion must be substituted for that premiss which next precedes the letter $k$, keeping the other premiss in its original situation.
g Again, to give another example in Bokardo,
$\sqrt{ }$ " Some good acts are not duly rewarded;"
" All good acts deserve to be rewarded:"
therefore," Some acts which deserve to be rewarded are not duly rewarded :"
reduced to Barbara thus,

[^50]
## SECTION VIII.

It has already been shown that syllogisms may be formed in twenty-four moods; viz. six in each figure: and in some one of these moods any conclusion may be inferred which can be drawn from a simple categorical syllogism ${ }^{\text {h }}$.

The same mood cannot always be used in The epecial every figure, see p . 102. without violating some one of the twelve rules given in Part III. Sect. III; hence certain special rules, or rather cautions, have been laid down with respect to all the figures, by a due observance of which a syllogism may be made in each figure without violating any rule.

## Special Rules of the First Figure.

Rule 1. The minor premiss must be affirmative.
For, if not, let it be negative, then the major mise afiriuapremiss must (by Rule $7^{\mathrm{i}}$.) be affirmative, and
${ }^{n}$ The number of moods in which any conclusion may be drawn are as follows:

A'may be proved in one mood only, viz. Barbara. $_{\text {s }}$
E may be proved in four moods, viz. Celarent, Cesare, $\boldsymbol{C a}$ mestres, and Camenes.

I may be proved in seven moods, viz. Darii and AII in the first figure, in Darapti, Disamis, Datisi, Bramantip and Dimaris.

0 may be proved in twelve moods, viz. Ferio and EAO in the first figure; in Festino, Baroko, and EAO, AEO in the second; in Felapton, Bokardo, and Ferison in the third; and in Fesapo, Fresison, and AEO in the fourth figure.
${ }^{1}$ The rules which are here alluded to are the twelve rules laid down in the third section of this Part.
will not distribute the major term; (because the major in this figure is the predicate of its premiss;) but the conclusion must (by Rule 8.) be negative, and will distribute its predicate, viz. the major term; and this term was shown not to have been distributed before ; hence there will be an illicit process of the major: consequently the minor premiss must not be negative, i. e. it must be affirmative ${ }^{k}$. Q. E. $\mathbf{D}$.

Major premiss aniversal.

Rule 2. The major premiss must be universal.
For, let it be particular, then its subject, which is the middle term, is not distributed; and by the last rule the minor premiss must be affirmative, consequently its predicate (which is the middle term) is not distributed; and it was shown not to be distributed in the major premiss: therefore the middle is undistributed. Therefore the major premiss must not be particular, i.e. it must be universal. ©. E. D.

## ${ }^{*}$ Thus, for example :

"Every true Christian is a lover of his God;"
" No atheist is a true Christian :"
therefore, " No atheist is a lover of his God."
This conclusion, although apparently correct, cannot be deduced from such premises; for the major term is distributed in the conclusion, which was not distributed in its premiss.
${ }^{1}$ Consequently the following argument is incorrect, because the middle term is not distributed:

[^51]
## Rules of the Second Figure.

Rule 1. One premiss must be negative.
For in the second figure the middle term is the
One premiss negative. predicate of both premises; consequently, if both were affirmative, the middle would not be distributed : therefore they must not be both affirmative, i. e. one premiss must be negative ${ }^{m}$. Q. E. D.
Rule 2. The conclusion must be negative. $\begin{gathered}\text { Concluaion } \\ \text { negative. }\end{gathered}$
Since one of the premises must, by the last Rule, be negative; hence (by Rule 8.) the conclusion also must be negative ${ }^{\text {D }}$. Q. E. D.

Rule 3. The major premiss must be universal. Major pre
The conclusion as has miss aniver-
The conclusion, as has before been shown, mal. must be negative; therefore the major term will be distributed in the conclusion; therefore it must also be distributed in the major premiss: but since in this figure it is the subject of its premiss, hence this premiss must not be parti-

- Thus, e. g.
" Every mail coach runs on four wheels;"
"Every barouche runs on four wheels ?"
therefore, " Every barouche is a mail coach."
This conclusion is manifestly false; for the middle term, being the predicate of two affirmative premises, is not distributed.
n Thus the following form of argument is incorrect, (by the 8th Rule of Sect. III.) because the conclusion is affirmative, one of the premises being negative :
" Every true patriot loves his country's welfare;"
" Some great statesmen do not love their country's welfare:"
therefore, " Some great statesmen are true patriots."
cular, or the major term would not be distributed, and there would be an illicit process of the major; therefore the major premiss must be universal ${ }^{\circ}$. Q. E. D.


## Rules of the Third Figure.

Minor premiss affirmative.

Conclusion particular.

Rule 1. The minor premiss must be affirmative. For, if not, let it be negative, then the conclusion must (by Rule 8.) be negative, and in it the major term will be distributed; but since the major premiss (by Rule 7.) must be affirmative, and the major term is the predicate of its premiss, therefore it is not distributed; consequently there is an illicit process of the major: therefore the minor premiss must not be negative, i. e. it must be affirmativep. Q. e. D.

Rule 2. The conclusion must be particular.
For since, by the last rule, the minor premiss must be affirmative, therefore the minor term

- Hence the following apparent syllogism is incorrect, for there is an illicit process of the major :
" Some pretenders to religion are deceitful;"
" No virtuous persons are deceitful:"
therefore, "Some virtuous persons are not pretenders to religion."
$p$ This case is similar to the first special rule of the first figure ; e. g .
" Every religious man is to be trusted;"
" No religious man is a hypocrite:"
therefore, " No hypocrite is to be trusted."
This form of argument is incorrect, for there is an illicit process of the major term.
(which in this figure is the predicate of its premiss) will not be distributed; consequently it must not be distributed in the conclusion: but if the conclusion were universal, the minor would be distributed; therefore the conclusion must not be universal; i. e. it must be particular ${ }^{\text {q }}$. Q. E. D.


## Rules of the Fourth Figure.

Rule 1. The major premiss must not be $\mathbf{O}$. For, if otherwise, let the major premiss $b e 0$, then the major term will not be distributed in its premiss ; but (by Rule 8.) the conclusion must be negative; and the major term will be distributed; therefore there will be an illicit process of the major: therefore the major premiss must not be $\mathrm{O}^{\text {r. }}$ Q. E. d.
${ }^{9}$ Thus, e.g.
" Every good deed is commendable;"
" Every good deed is a virtuous act:"
therefore, " Every virtuous act is commendable."
In this apparent syllogism the minor term, " virtuous act," is distributed in the conclusion, and not in the premises; consequently there is an illicit process of the minor: and it may be observed, that since the minor premiss is affirmative, the minor term cannot be distributed in its premiss in any mood in the third figure; hence the conclusion must be particular.
$r$ Hence the following form of argument is not correct:
" Some men of good understanding are not led astray by prejudice;"
"All who are led astray by prejudice are liable to commit frequent mistakes:"
therefore, "Some who are liable to commit frequent mistakes are not men of good understanding."

Major premiss not $O_{\text {, }}$

[^52]


Rule 2. The minor premiss must not be $O$.
For, if otherwise, let the minor premiss be $\mathbf{O}$, then (by Rules 7 and 10.) the major premiss must be A , and the middle term (which is the predicate of the major and subject of the minor premiss) will not be distributed; therefore the minor premiss must not be $O^{\text {: }}$. Q. e. d.
Rule 3. The conclusion must not be $A$.
For, if otherwise, let the conclusion be A; then (by Rules 8 and 11.) the premises must both be A; but in the conclusion, the minor term will be distributed, which was not distributed in its premiss: therefore there will be an illicit process of the minor: therefore the conclusion must not be $\boldsymbol{A}^{\mathbf{t}}$. Q. E. D.

In this case it is manifest that there is an illicit process of the major term.

- Thus, e.g.
" Every just man is a subject worthy of admiration:"
"Some who are subjects worthy of admiration are not to be despised :"
therefore, " Some who are to be despised are not just men."
In this case the middle is not distributed; consequently such a form of argument is not admissible.
- In order to draw an universal affirmative conclusion, the premises must both be universal affirmative, thus:
" Every good razor is sharp;"
" Every sharp instrument is a dangerous weapon in unskilful hands:"
therefore, " Every dangerous weapon in unskilful hands is a razor."
This apparent syllogism is manifestly incorrect, for there is an illicit process of the minor term.
The following Table presents, at one view, all the special rules, with their proofs.


## Proofs.

Minor premiss affirmative . . . . . . . . . Or, illicit process of the major.
Or, middle not distributed.
Or, middle not distributed.
Because of the negative premiss.
Or, illicit process of the major.
Or, illicit process of the major.
Or, illicit process of the minor.
Or, illicit process of the major.
middle not distributed.
Or, illicit process of the minor.
: $\cdot$ .



 -• -






-





- [esazatun ssturad rofend
One premiss negative . . Conclusion negative .
Major premiss universal
Minor premiss affirmative Major premiss not $\mathbf{O}$.
$\infty$
Figure.
1
N
4
Conclusion not A

To find a middle term.

Hence it is manifest with what middle term any conclusion may be proved; e.g. To prove a particular affirmative conclusion, a middle must be brought forward, which is wholly contained by one extreme, and which itself contains a part of the other, (as in the first figure,) or, by a middle term which represents that of which both the extremes are qualities, (as in the third figure,) or, lastly, by a middle which comprehends one extreme, and is itself comprehended under that class of which the other extreme is a part, (as in the fourth figure ${ }^{\text {u }}$.)
N. B. (1.) A nameless mood ought not to be brought forward to prove a conclusion; for, since the conclusion is particular, when it ought to
a Care should be. taken that more be not laid down in the premises, than is absolutely necessary to prove the conclusion; for this would give an opponent an opportunity of raising an objection, when it might easily be avoided; e. g.
" All planets are more distant than the moon;"
" All planets can be seen from the earth :"
therefore, " Some bodies which can be seen from the earth are more distant than the moon."
In this syllogism, an objection might be raised against the minor premiss, because it might be argued, that possibly " some planets could not be seen from the earth;" and this objection might be obviated by making the minor premiss particular, without any detriment to the syllogism ; hence, in this argument, more is laid down in the premises than is necessary for proving the conclusion; it is on this account that Darapti and Felapton are not so accurate as either Disamis, Datisi, Bokardo, or Ferison; so in the fourth figure, Bramantip and Fesapo are less accurate than Dimaris and Fresison; because the premises need not be both universal, in order to prove a particular conclusion.
have been universal, hence more has been laid down in the premiss than was necessary for proving the conclusion.
(2.) Of all the four figures, the fourth is the worst, for it is the most unnatural of all, and in it the middle is (by implication) predicated of itself, thus ${ }^{\mathrm{x}}$ :
> " Every wise man is contented;"
> " Every contented man is happy :"
> therefore, " Some happy men are wise."

In this syllogism, the middle term contented, is predicated of every wise man; this, in the conclusion, is predicated of the minor, happy man; and this minor, happy man, is predicated in the minor premiss of the middle contented: consequently the middle is, by implication, predicated of itself Y .

[^53]
## SECTION IX.

Of enthy- 1. The enthymeme is a defective syllogism,

Different kinds of arguments. meme.

There are many other kinds of arguments, which are not correct syllogisms, yet may easily be brought into the regular form, such as the following: which consists of one premiss and a conclusion; e.g.
" Diamonds are jewels; they are therefore valuable."
" God is a spirit; therefore he is eternal."
An enthymeme may easily be reduced to aregular syllogistic form; for since the conclusion and one premiss are given, the three terms may be known, and the omitted premiss may be supplied: thus, in the above example, the major, " All jewels are valuable," is omitted, (see p. 75, note b.) and, if supplied, the syllogism will be regular ${ }^{2}$, thus :
$=$ In common discourse the usual mode of expressing an argument is by means of the enthymeme; it being unnecessary to adduce both the premises, when one is so evident that it may very fairly be left to the hearer's judgement; e. g.
" When we find a book quoted, or referred to by an ancient author, we are entitled to conclude that it was read and received in the age and country in which that author lived." This sentence is an enthymeme, in which the major premiss is suppressed, but which may easily be supplied as follows: " Every book quoted, or referred to by an ancient author, must have been read and received in the age and country in which that author lived." The sentence may thus be reduced to a

> "All jewels are valuable ;"
> " Diamonds are jewels:"
> therefore, " Diamonds are valuable."

Again :
" Every spirit is eternal ;"
" God is a spirit: :"
therefore, " God is eternal."
In both these examples, the major premiss is suppressed; for, as was before observed, the major premiss is, generally speaking, some universal and incontrovertible principle, which is so evident that it is left to the hearer's judgement ; but the minor premiss is most commonly expressed, because it has more particular reference to the question which is to be proved ${ }^{\text {a }}$; (see p. 85, note p.)

An enthymeme is sometimes condensed into one sentence, which is called an enthymematic sentence; viz. when the premiss is united in one proposition with the conclusion; e. g. "All
regular syllogism in Barbara : this may be effected in most enthymemes without much difficulty, whether their conclusions be negative or affirmative.
a Although the major premiss is generally suppressed in most enthymemes, yet there are some enthymemes in which the minor premiss is found to be omitted; this may happen when the minor premiss is very evident, or when much stress is meant to be laid upon the major ; e.g. "Every tyrannical king deserves to be deposed by his subjects; therefore Nero deserved to be deposed by the Romans." The minor premiss which is suppressed, may be thus supplied:
" Nero was a tyranical king ;"
and thus the argument is reduced to the regular syllogistic form.
machines, being of human manufacture, are liable to imperfections." This argument may be thus expanded into a regular syllogism:
" All things of human manufacture are liable to imperfections;"
" All machines are of human manufacture:" therefore, "They are liable to imperfections ${ }^{\mathrm{b}}$."
2. Induction is the inferring an universal conclusion from a great number of particular facts; i.e. when any fact has been ascertained with respect to a great many individuals of a class, by induction, we infer that the same fact is predicable of all that class ${ }^{\text {c }}$.
${ }^{6}$ The following are some examples of enthymematic sentences: "Is an enterprise fraught with evil, such as the present, likely to prosper ?" This question may thus be reduced to a syllogistic form :
"An evil enterprise is not likely to prosper;"
" The present enterprise is evil :"
therefore, " The present enterprise is not likely to prosper."
Again: "Useful knowledge is too difficult of attainment to be within the reach of the idle."
This sentence may be thus syllogistically expressed :
$\sqrt{ }$ " Nothing which is difficult of attainment is within the reach of the idle;"
" All useful knowledge is difficult of attainment:"
therefore, " Useful knowledge is not within the reach of the idle."
This is a regular syllogism in Celarent.
e Thus Dr. Whately, in the preface to his "Elements of Logic," proves by means of an inductive argument, that " Mankind universally bear their testimony, though unconsciously and often unwillingly, to the preferableness of syste-matic knowledge to conjectural judgements." He shows that this is the case in many sciences, which he enumerates, proving

Thus by induction we may infer that all bodies are liable to fall towards the centre of the earth, because we perceive this fact to exist the same, under similar circumstances, in all bodies upon which we make the experiment. This inference is, as Dr. Whately very justly observes, "a syllogism in Barbara, with the major suppressed; that being always substantially the same, as it asserts, that 'what belongs to the individual or individuals we have examined, belongs to the whole class under which they comed.'" The above example may thus be reduced to a syllogistic form, in Barbara :
"That quality which is perceived to exist in many bodies, is Example of likely to exist in all;" induction.
"The liability to fall towards the centre of the earth, is a quality which is perceived to exist in many bodies:"

Therefore, "The liability to fall towards the centre of the earth, is a quality which is likely to exist in all bodiese."

It is by induction that almost all elementary
that every man " Gives the preference to unassisted common sense only in those cases where he himself has nothing else to trust to, and invariably resorts to the rules of art, wherever he possesses the knowledge of them." He then infers the universal conclusion, that " Systematic knowledge is preferable to conjectural judgement."
d See Elements of Logic.

- The great error into which induction is likely to lead us, is a too great haste in drawing the conclusion; viz. the inferring an universal conclusion, when the facts enumerated are not sufficient in number to authorise such an inference: in order to make a correct induction, the number of facts must be very great; and the greater the number, the more perfect will be the induction.
principles are proved: indeed, they do not admit of any other mode of proof; and a perfect induction is as decisive an argument as even demonstrable evidence: thus, when a stone is thrown into the air, I am as convinced that it will fall to the ground, (even though I should not see it,) as if it were demonstrated to me by the most incontrovertible evidence ${ }^{f}$.

Example.

Difference between evample and induction.
3. The example is, when from a knowledge that any fact has occurred, we infer that the same event will take place with respect to some other unknown fact.
There are two points in which the example differs from induction.
(1.) With respect to the premises; for in induction the facts from which we draw the universal conclusion must be very many in number; whereas in example, we may draw our conclusion from one single fact.
(2.) With respect to the conclusion; for in induction the conclusion is universal, and the

[^54]inference drawn is, that the same fact will always happen the same under similar circumstances; but in example this is by no means the case, for the conclusion does not infer the certainty of any fact occurring in the same manner as the one similar fact from which we draw our conclusion, but merely the probability of such an occurrence ${ }^{8}$; and the degree of this probability will of course depend on the number of similar facts which are adduced, in order to show that the particular fact in question will probably occur. The more facts that we can adduce, the more does the example approach the induction, and the greater degree of probability will its conclusion possess.
4. The sorites is a number of syllogisms, in Sorite.

[^55]which the conclusion of each is made a premiss of the next, and so on, till we arrive at the last; but in the sorites these syllogisms are not given at full length, for the conclusion of each syllogism is suppressed; so that the form of the sorites becomes a number of propositions, in which the predicate of each becomes the subject of that which follows: thus, e. g. "Every good man lives in the fear of God;" "Every man who lives in the fear of God is virtuous;" " Every virtuous man is contented;" " Every contented man is happy:" therefore, "Every good man is happy ${ }^{\text {h." }}$

This sorites may thus be placed in a regular syllogistic form :
(1.) "Every man who lives in the fear of God is virtuous;"
" Every good man lives in the fear of God:"
therefore, " Every good man is virtuous."
(2.) "Every virtuous man is contented;"
" Every good man is virtuous:"
therefore, "Every good man is contented."
${ }^{\text {h }}$ A sorites is nothing more than a number of condensed syllogisms, which may easily be expanded, so as to be in the regular form : it does not require any reduction, for it is already in the first figure, although it may appear to be in the fourth, because the premises are transposed. "It is to be observed," says Dr. Whately, " that the enthymeme is not syllogistic ; i. e. its conclusiveness is not apparent from the mere form of expression, without regard to the meaning of the terms; because it is from that we form our judgement as to the truth of the suppressed premiss. The sorites, on the other hand, is strictly syllogistic."-Elements of Logic.
(3.) "Every contented man is happy;"
" Every good man is contented:"
therefore, " Every good man is happy."
Thus it may be observed, that the sorites is a series of syllogisms in the first figure, in which the premises are transposed.

Hence it follows, that in a sorites only one Only one prepremiss can be negative ${ }^{i}$; for in this case one of $\begin{gathered}\text { miss } \\ \text { nege onaiive } \\ \text { and }\end{gathered}$ its syllogisms would have both of its premises negative; neither can any more premises than one be particular; for then, as before, one of its syllogisms would have both its premises particular.
5. The prosyllogism is a proposition which prosyllois attached to one of the premises, as it were incidentally, to confirm the strength of that premiss; in fact, the premiss, to which the prosyllogism is attached, is the conclusion of an enthymeme, of which the prosyllogism itself is the premiss; e.g.
" Every virtuous act is worthy of commendation;"
" Every act of charity, (if it proceeds from a mind actuated by proper principles,) is a virtuous act:"
therefore, " Such acts of charity are worthy of commendation."
1 Thus the following sorites is incorrect:
" Every man is endued with the faculty of reasoning; No animal endued with this faculty is a brute; No brute has the power of speaking; Every being who has the power of speaking has also the power of communicating to others his ideas: therefore, Every man has the power of communicating to others his ideas." It will also be easy to show that the negative premiss, which is allowable in a sorites, must be the last premiss; and the particular premiss (if there be one) must be the first: these rules will be manifest by trying examples.

Sometimes used as a premiss.

The prosyllogism is not uncommonly used instead of that premiss of which it is the proof ${ }^{k}$; and from this circumstance the syllogism, though correct, would seem to have too many terms: thus, in the following example.
$\sqrt{ }$ " Charity covereth a multitude of sins;"
" A multitude of sins is a load of evil :"
therefore, " Charity covereth a load of evil."
This syllogism may, at first sight, appear to be faulty, because there are apparently five terms; but it may be shown to be correct, thus:
" That which covereth a multitude of sins covereth a load of evil: (for a multitude of sins is a load of evil;)"
" Charity covereth a multitude of sins:"
therefore, " Charity covereth a load of evil."
${ }_{k}$ This is frequently put into practice, in order to condense the argument; the same circumstance may be frequently observed in the sorites, where two or three prosyllogisms are sometimes employed instead of their premises ; e. g. "The sun is a created thing; those who worship a created thing are guilty of idolatry; those who are guilty of idolatry act under mistaken notions : therefore, those who worship the sun act under mistaken notions." This sorites may easily be brought into an accurate syllogistic form, (though its present form is not strictly regular,) as follows:
"Those who worship a created thing are guilty of idolatry;"
" Those who worship the sun worship a created thing, (for the sun is a created thing:)"
therefore, "Those who worship the sun are guilty of idolatry."
"Those who are guilty of idolatry act under mistaken notions;"
" Those who worship the sun are guilty of idolatry :"
therefore, "Those who worship the sun act under mistaken notions,"

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Thus the prosyllogism, " a multitude of sins is a load of evil," is substituted for the major premiss, the truth of which it was intended to confirm.
6. It is a common practice to suppress the Suppresered conclusion ${ }^{1}$ at the end of any argument; and this ${ }^{\text {conclasion. }}$ is very frequently done in common conversation, as well as in argumentative writings; for the conclusion being known from the question, it would be useless to express it at the close of every argument. This practice is not confined to opponents ${ }^{\mathrm{m}}$ only, but is done by all who are engaged in discussing any subject.

The following arguments are given by way of practising the student in detecting the errors which may be found in apparent syllogisms: those which are correct may be reduced, if necessary:

1. Some good men are happy;

All virtuous men are good;
Some virtuous men are happy.
2. Every mail coach keeps good time ;

Every good musician keeps good time ;
Every good musician is a mail coach.

[^56]3. No human being is perfectly happy ;

No horse is a human being;
No horse is perfectly happy.
4. No man can servè two masters ;

I am a man;
I cannot serve two masters.
5. Many men have many minds;

You are a man ;
You have many minds.
6. Reason is the peculiar characteristic of man; There is reason in roasting eggs ;
The peculiar characteristic of man consists in the faculty which he possesses of roasting eggs.
7. A true friend is not often to be met with;

That which is not often met with is generally valuable;
A valuable thing is a true friend.
8. Nothing is more rare than disinterested friendship;

That which is more rare than disinterested friendship is precious;
Nothing is precious.
9. Nemo mortalium omnibus horis sapit;

Ego sum mortalis;
Non omnibus horis sapio.
10. Qui sapit pauca loquitur;

Pauca loquor ;
Sapio.
11. No profane swearers are to be believed on their oath ;

All men who are to be believed on their oath are worthy of being received as witnesses ;
No men who are worthy of being received as witnesses are profane swearers.
12. All tulips are beautiful flowers;

No thistles are tulips;
No thistles are beautiful flowers.
13. No liar is worthy of credit;

All liars are dishonourable;
No dishonourable man is worthy of credit.
14. Three and two are five;

Three and two are odd and even;
Five is odd and even.
15. All men are animals;

I am an animal ;
I am a man.
16. All astronomers are men ;

Some philosophers are astronomers ;
All philosophers are men.
17. Some men are wise;

All men are animals;
Some animals are wise.
18. Some quadrupeds cannot fly ;

I cannot fly;
I am not a quadruped.
19. No brute is a man;

No dog is a man;
Every dog is a brute.
20. Omnis equus est bestia;

Omnis justus est æquus;
Omnis justus est bestia.
21. Nothing mortal is incorruptible ;

The soul of man is incorruptible;
The soul of man is immortal.
22. Dionysius was a tyrant ;

Buonaparte was a Dionysius;
Buonaparte was a tyrant.
23. Six and five are even and uneven ;

Eleven are six and five;
Eleven are even and uneven.
24. Every sword is an instrument of war ;

No ploughshare is a sword;
No ploughshare is an instrument of war.
25. Some countries are hot;

Some countries are cold;
Some cold countries are also hot.
26. No quadrupeds are bipeds;

A man is not a quadruped;
A man is not a biped.
27. Finis rei est illius perfectio;

Mors est finis vitæ ;
Mors est vitæ perfectio.
28. To kill a man is a sin ;

To hang a murderer is to kill a man;
To hang a murderer is a sin.
29. Whatever is immaterial is incorruptible ;

An angel is immaterial;
An angel is not corruptible.
30. Some razors are not sharp ;

All sharp things are apt to cut;
Some things apt to cut are not razors.
31. All philosophers are men ;

All philosophers are rational ;
All rational beings are men.
32. Some men are astronomers;

No astronomers are fools ;
Some fools are not men.
33. All men are corporeal ;

No angels are men;
No angels are corporeal.
34. All men breathe ;

I breathe;
I am a man.
35. Some Christians are pious;

All pious men are good;
All good men are Christians.
36. All created things are corruptible ;

The Deity is uncreated;
The Deity is incorruptible.
37. Some cities are fortified;

Oxford is a city ;
Oxford is fortified.
38. All true Christians are lovers of God;

Some lovers of God are Englishmen ;
Some Englishmen are true Christians.
39. Nemo mortalium omnibus horis sapit;

Ego nunquam sapio;
Ego non sum mortalis.
40. Sophocles was a Greek tragedian ;

Euripides was not Sophocles;
Euripides was not a Greek tragedian.
41. All statesmen are men of learning;

All men of learning are wise;
All wise men are statesmen.
42. Charity covereth a multitude of sins ;

A multitude of sins is a load of evil;
Charity covereth a load of evil.
43. Every good man is a worthy character ;

Every good man is a religious man;
Every religious man is a worthy character.
44. Humanum est odisse quem læseris;

Irasci est humanum;
Irasci est odisse quem læseris.
45. Every turbulent demagogue is to be feared;

Every turbulent demagogue should be kept in order by the force of the law;
All who are to be feared should be kept in order by the force of the law.
46. Every art is useful;

Logic is an art;
Logic is not useful.
47. That which is not true relates what is not the fact;
A falsehood does not relate what is the fact;
A falsehood is not true.
48. He that calls you an animal speaks the truth ;
He that calls you a goose calls you an animal;
He that calls you a goose speaks the truth.
49. Some penknives are sharp;

Some razors are not sharp ;
Some razors are not penknives.
50. A watch is a machine intended for showing the time;
A sentinel is a watch;
A sentinel is a machine intended for showing the time.

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51. That which is worth gaining cannot be attained without labour;
All useful knowledge is worth gaining ;
No useful knowledge can be attained without labour.
52. The thoughts of men are unfathomable;

The depth of the sea is unfathomable;
The depth of the sea is the same as the thoughts of men.
53. A tree is not a sentient being;

No man is a tree;
A man is a sentient being.
54. A tale is a short history ;

The limb of some animal is a tail;
The limb of some animal is a short history.
55. All fire burns;

Ice is not fire;
Ice does not burn.
56. Some cities are not fortified;

All fortified places are fortresses ;
Some fortresses are not cities.
$V_{57}$. All papists believe the pope to be infallible;
The pope is a man ;
All papists believe a certain man to be infallible.
58. No man is infallible;

The pope is a man;
The pope is not infallible.
59. Love is a species of madness ;

You are in love ;
You are mad.
60. Every beautiful object is worth beholding ;

A fine view is worth beholding;
A fine view is a beautiful object.
61. Gallus est homo ;

Volucris quidam est Gallus ;
Volucris quidem est homo.
62. Every Englishman will fight for his country ;

All those who will fight for their country are brave men;
All brave men are Englishmen.
63. An art is a collection of rules leading to some certain end;
Logic is a collection of rules leading to some certain end;
Logic is an art.
64. Emulation deserves to be promoted;

Emulation may lead to the production of evil passions;
Every thing which may lead to the production of evil passions deserves to be promoted.
65. He that spareth the rod hateth his child;

An affectionate parent does not hate his child;
An affectionate parent does not spare the rod.
66. Every book is liable to error ;

Every book is a human production;
All human productions are liable to error.
67. Some detestable vices are not abhorred as they deserve;
Malice is a detestable vice;
Malice is not abhorred as it deserves.
68. He that has a good understanding leads a truly Christian life ;
All who lead a truly Christian life may be deemed really wise;
All who may be deemed really wise are men of good understanding.
69. Virtue graces those who possess it ;

Those who possess it are to be envied;
Virtue graces those who are to be envied.
70. Every amiable person gains the affections of his neighbours;
Those gain the affections of their neighbours who are charitable;
Every charitable person is amiable.
71. Six and two are eight;

Five and three are eight;
Five and three are six and two.
72. Some animals are birds;

All winged beings are animals;
Some winged beings are birds.
73. Those who are apparently religious, and really are not so, are not to be trusted;
Hypocrites are not to be trusted;
Hypocrites are those who are apparently religious, and really are not so.
74. No spirits are mortal beings;

All immortal beings are incorruptible;
No mortal beings are spirits.
75. Every wise man bridles his tongue;

Those who do not bridle their tongue are liable to be involved in quarrels;
Those who are liable to be involved in quarrels are not wise.
76. Every innocent thing is allowable;

Some pleasures are allowable;
Some pleasures are innocent.
77. Every innocent thing is allowable;

Some pleasures are not innocent;
Some pleasures are not allowable.
78. Nothing is more to be dreaded than a false friend;
Many false friends are pleasant companions ;
Many pleasant companions are to be dreaded.
79. Those who are not acquainted with the rules of logic are not good logicians ;
Schoolboys are not acquainted with the rules of logic;
Schoolboys are not good logicians.
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80. Every conceited man is vain;

Every vain man is a fool ;
All fools are conceited.
81. A definition is intended to explain ;

An illustration is intended to explain;
An illustration is a definition.
82. No man can serve two masters;

A dog is not a man ;
A dog can serve two masters.
83. Water is ornamental ;

Rain is water;
Rain is ornamental.
84. No quadruped has the power of flying;

A man is not a quadruped;
A man has not the power of flying.
85. Some species of gases are inflammable;

Balloons are filled with gas;
Balloons are inflammable.
86. Every good king deserves the love of his subjects;
George the Fourth is a good king ;
George the Fourth deserves the love of his subjects.
87. No brute degrades itself by eating or drinking to excess ;
Some men do thus degrade themselves;
Some men are not brutes.
88. Idleness generally leads to a bad end;

Hard labour is not idleness;
Hard labour does not lead to a bad end.
89. Those who work hard deserve reward; Those who work on the treadmill work hard; Those who work on the treadmill deserve reward.
190. All meteors are vapours; Some vapours are luminous; Some luminous bodies are meteors.
91. A dutiful son loves his parents ; A spendthrift is not a dutiful son; A spendthrift does not love his parents.
92. He who lives beyond his income is thoughtless; Many men at Oxford live beyond their income; Many men at Oxford are thoughtless.
-93. A brute is not an immortal being; All immortal beings are incorporeal ; No incorporeal beings are brutes.
94. That which is naturally an inherent quality cannot be changed by the power of art;
It is a natural quality inherent in animals to love themselves;
This quality cannot be changed by the power of art.

95 . He who is worthy of confidence ought to be possessed of prudence;
He who is possessed of prudence is also possessed of every virtue ;
He who is possessed of every virtue is worthy of confidence.
96. No man of honour is addicted to equivocation ; He who is guilty of equivocation is not to be trusted;
He who is not to be trusted is not a man of honour.
97. Many languages are difficult to learn;

Greek is a language ;
It is difficult to learn.
98. A sorrowful countenance is by no means the characteristic of a religious man.
A sorrowful countenance indicates a heart not at ease;
That which indicates a heart not at ease is not the characteristic of a religious man.
99. Those who are inexperienced in the ways of life, and are under the influence of their passions, are not fit to study moral philosophy ;
Such are all young men ;
They, therefore, are not fit to study moral philosophy.
100. Every prudent parent governs his family properly, and is anxious for the welfare of its members;
Many parents do not act thus ;
Many parents are not prudent.
101. All human institutions are imperfect;

The laws of England are a human institution ;
The laws of England are not perfect.
102. A mean artifice is beneath the notice of a man of strict honour ;
Calumny is beneath the notice of a man of honour;
Calumny is a mean artifice.
103. The characters of some men, though of the most detestable description, are unknown to the rest of the world;
Many things which ought to be revealed are unknown to the rest of the world;
Some things which ought to be revealed are the characters of some men.
104. Many men have common sense;

Some men have uncommon sense;
Some who have uncommon sense have also common sense.
105. No man can have two opinions on the same subject;
Some men are not very wise ;

Some who are not very wise, have not two opinions on the same subject.
106. Some persons, although men of the greatest learning, have committed errors ;
All persons, who are men of sense, are not so liable to err as those who are foolish;
Some who are not so liable to err as those who are foolish, have nevertheless committed great errors.
107. Some animals live upon the blood which they obtain from others;
All animals are sensitive beings;
Some sensitive beings live upon the blood which they obtain from others.
108. All men are bound to act according to the strictest rules of virtue;
No brutes are men;
No brutes are bound to act according to the strictest rules of virtue.
109. All minerals are produced under ground ;

Potatoes are produced under ground;
Potatoes are minerals.
110. All vices ought to raise the indignation of every good man ;
A praiseworthy act is not a vice;
A praiseworthy act ought not to raise the indignation of any good man.
111. No human virtue is wholly free from imperfections;
Many benefits have accrued to mankind by means of human virtues;
Many benefits have accrued to mankind by means of things not wholly free from imperfections.
112. He that is placed in the highest sphere of life is not more exempt from death than he that is placed in the lowest;
Not even the lowest man should forget that he is mortal ; therefore,
He that is placed in the highest sphere ought not to forget that he is mortal.
$\sqrt{ } 113$. John is taller than Richard;
Richard is taller than Thomas;
John is taller than Thomas.
114. An unintentional insult should be immediately forgiven ;
An act which demands immediate forgiveness is sometimes a good act;
Some good act is an unintentional insult.
115. He who wastes his time is ignorant of its value;

No man who employs himself in the acquisition of useful knowledge, wastes his time;
Such a man, therefore, is not ignorant of its value.

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116. He who is wise in his own conceit is generally a fool;
A fool is most commonly troublesome;
Some troublesome people are wise in their own conceit.
117. Those who suspect others without just reason are liable to suspicion themselves;
Those who are liable to suspicion are frequently no better than they should be;
Those who suspect others are frequently no better than they should be.
118. Some good intentions are not strictly consistent with prudence;
Every good intention is worthy of commendation;
Some acts which are worthy of commendation, are not strictly consistent with prudence.
119. No vegetable is a mineral ;

All minerals are subterraneous productions;
No subterraneous productions are vegetable.
120. A true friend is an honest man;

An honest man is an estimable character ;
Some honest man is a true friend.
121. Every wilful transgression of the laws deserves proper punishment;
Proper punishment has generally a good effect;
Every wilful transgression of the laws has generally a good effect.
122. Nothing is more disagreeable than the selfishness discernible in some-persons; for the selfish man is so wholly taken up with himself, that he cares but little for the inconvenience to which he exposes others.
123. Haste makes waste, waste makes want, want makes a rich man poor; therefore, Haste makes a rich man poor.
124. Friends should not be purchased by presents; for a friendship established on such a foundation will most commonly end when the power of making those presents shall cease.
125. What being can be more wretched than the miser? he is always in want and is never satisfied.
126. Blessed are the poor in spirit, for theirs is the kingdom of heaven.
127. George the Fourth is a good king, a good king is deserving of esteem, (for good kings are scarce,) those who deserve esteem are worthy of our love; therefore, George the Fourth is worthy of our love.
128. The ascent in a balloon is not attended with any very considerable danger or difficulty, for Mr. Green has, within a few years, made upwards of sixty ascents, and has, on all occasions, landed without serious injury.
$\sqrt{129}$. "Now controversy being almost always either the offspring or the parent of party, it is not wonderful that a love of disputation should almost always either give occasion to, or exasperate, party spirit." - Dr. Whately's Bampton Lectures.
130. "That there are subjects connected with religion, which it is unprofitable or worse than unprofitable to discuss, no one would venture to deny; and it is no less undeniable, that among these are to be reckoned such as are neither laid open to us by revelation, nor are comprehensible by our reason: but men are, in general, far less ready practically to conform to this maxim, than to admit its truths."-Ibid. !
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[^0]:    * Any one word (whether representative of a simple or a compound idea) denotes an incomplex simple apprehension in its logical sense. So also any number of words when combined sb as to form a sentence, become representatives of complex apprehension.
    b Dr. Whately defines judgement to be "The comparing together in the mind two of the notions (or ideas) which are the objects of apprehension, whether complex or incomplex, and pronouncing that they agree or disagree with each other; (or that one of them belongs or does not belong to the other.)" He thus considers the comparison as much a part of judgement as the decifion itself-whereas the latter is the result

[^1]:    of the former : for the object of comparison is to pronounce a judgement on the relations which the objects compared may have to each other.

[^2]:    e Care must be taken not to confound reason with reasoning. For reason, in its common acceptation, signifies "That use of the faculties of the mind which distinguishes man from any other animal," viz. " It is the characteristic of man." But reasoning, or ratiocination, (discursus,) is " the process of inferring a proposition or conclusion, as necessarily resulting from one or more other propositions."

[^3]:    "The words "mendosa collectio" do not exactly mean " erroneous inference," as they are most frequently translated; but rather " a faulty arrangement of the terms of an argument." This will be more clearly shown in the third part of logic.

    - "It is to be observed, however, (says Dr. Whately), that as a science is conversant about knowledge only, an art is the application of knowledge to practice: hence logic (as well as any other system of knowledge) becomes, when applied to practice, an art ; while confined to the theory of reasoning, it is strictly a science: and it is as such that it occupies the higher place in point of dignity, since it professes to develop some of the most interesting and curious intellectual phenomena. It is surely strange, therefore, to find in a treatise on logic, a distinct dissertation to prove that it is an art and not a science!"

[^4]:    ${ }^{5}$ Few sciences have fallen into such disrepute as that of logic, the sole cause of which has been the error into which even logicians themselves have fallen respecting the true nature of it; and thus the censure, due to those who caused the error, has fallen upon the science itself. Many have supposed that logic was a science, the object of which would be the attainment of knowledge; and "Accordingly many logical writers, wishing to make their systems appear as perfect as possible, have undertaken to give rules 'for attaining clear ideas,' and 'for guiding the judgement;' and fancying, or professing themselves successful in this, have consistently enough denominated logic the 'art of using the reason;' which in truth it would be, and would supersede all other studies, if it could of itself ascertain the meaning of every term, and the truth or falsity of every proposition, in the same manner as it actually can, the validity of every argument."-Elements of Logic. Logic lays down certain rules as tests of the validity of any argument, as far only as the form of its expression is concerned. It does not profess to communicate any knowledge, but to guide and direet the mind in the acquisition of knowledge. It cannot supply mental faculties to those who have them not, so neither could an eyeglass make a blind man see. All arguments can ultimately be applied to the tests which logic has laid down, and by them their validity or fallacy may be ascertained.

[^5]:    E Words are merely arbitrary signs, and they do not naturally possess any fitness in their sound or form, as necessary in order that they should express the ideas or objects intended. If this were the case, all languages would have the same words to express the same ideas, which is not the case. For the same sound conveys different ideas in different languages, and not only in different but in the same language, as is the case with equivocal words.

[^6]:    ${ }^{h}$ Aldrich.
    ${ }^{1}$ Since (from the definition of judgement) the word expressive of it must consist of some combination of simple words, hence has arisen the term complex word. Also since the word

[^7]:    1 " It is worth observing, that an infinitive (though it often comes last in a sentence) is never the predicate, except when another infinitive is the subject."-Whately.
    The Greek examples, which have been given, are instances of the truth of this observation.

[^8]:    - A categorematic word need not be one grammatical word; e. g. "Man that is born of a woman hath but a short time to live." "Man - that - is - born - of - a - woman" is the subject, and is one categorematic word, and " a - being - that - hath - but - a - short - time - to - live" is the predicate, and is also only one categorematic word.

[^9]:    n This fact is denied by Dr. Whately; but I am of opinion, that an adjective cannot ever be strictly said to be the predicate of a proposition : and this may be shown to be the fact, by converting a proposition in which the predicate is expressed adjectively; e.g. "Some men are learned;" the simple converse of which is, "Some learned beings are men :" in which " beings," or some such word, must be expressed in order that the proposition, when converted, may be grammatical. Now since conversion is the transposition of the extremes of a proposition without any change in the extremes themselves, the word "beings" must have been implied, though it was not expressed, in the predicate of the converted proposition.

[^10]:    - The words " recta vox" [Aldrich, c. 1. § 3.] signify " a word in the nominative case;" for grammarians considered the form of the noun as erect or upright; i. e. "rectus;" and the various changes which that noun received in government, they considered as "fallings down" (or "casus") from that uprightness. Hence the other cases were termed oblique.

    P A more accurate definition would be, a logical noun is " a word which is significant, and inexpressive of relation or time." Thus excluding adjectives and nouns in oblique cases.
    4. The division of nouns into singular and common is the true

[^11]:    r The particle non is consequently called indefinitant; because when prefixed to a noun, it renders that noun indefinite. For the use of the definite and indefinite nouns in division, see note on th: subject in Sect. VII.

[^12]:    - Thus the word dog is an univocal word, and is applicable in the same signification to many dogs: equivocal words are such as are the same in sound, but convey different ideas; as the words mail, which signifies armour, and the post-bag; and page, which signifies either the side of a leaf in a book, or an attondant. Fallacies often result from using such words; these fallacies are termed "fallacie equivocationis."-Whately.

[^13]:    y Singular nouns, which denote any one individual object, cannot be affirmatively predicated of anything except themselves, i. e. they cannot be the predicate of any affirmative proposition, unless its subject be a word expressive of that same individual object which the singular noun represents; thus, this university and Oxford are singular nouns, which cannot be predicated of anything but themselves; for we may say, this university is Oxford, but we cannot predicate of any other university that it is Oxford. Singular nouns may be used as the predicate of any negative proposition, whose subject does not express the same individual object, e.g. London is not Oxford, \&c.

    Common nouns denote a whole class, and any individual in that class; and consequently may be predicated of all or of any one, of those individuals; thus university, city, are common nouns; and we may predicate of Oxford that it is an university, or that it is a city; for Oxford is an individual which is compreliended under each of those common nouns.

[^14]:    : When in contemplating any individual object, we consider any onè property or quality which that individual may possess, to the exclusion of all its other qualities, we are said to abstract this quality; thus, if in looking at any individual horse, we should regard only the property of his having four legs, excluding all thoughts respecting his colour, height, temper, \&c. we should be employing the faculty of abstraction : but if we contemplate many horses, and from finding that they are all four-legged animals, we give to them a common name, which may (as far as they agree with each other) be applicable to all or each of them, (as, quadruped), we are then employing what is termed generalization. Such generalization may obviously be carried to almost any extent by considering such common nouns (as, for instance, quadruped), as singulars; and by abstracting their differences, we shall thus arrive at new aggregates, and at some more universal term : thus by abstraction from quadruped we should arrive at the more common term animal; so from animal we should gain the still more universal term corporeal being, and so on.

[^15]:    a The idea expressed by a common term is (as Dr. Whately observes) " merely an inadequate (or incomplete) notion of an individual; and from the very circumstance of its inadequacy, it will apply equally well to any one of several individuals :" e.g. if I, when considering Oxford, were to omit all consideration of any of those circumstances and accidents which are peculiar to Oxford, and distinguish it from any other city, the notion which I have thus formed of Oxford, (which is expressed by a common term city), is evidently an inadequate and incomplete notion of it, for such common term is as applicable to any other city as to Oxford; and, therefore, inadequately expresses it, because it does not imply or designate any of its peculiarities.

[^16]:    d Properties are those qualities which are predicated of any essence as necessarily joined to it; but it must not therefore be supposed, that no property can be separated from its essence; for this may frequently be the case, particularly with such properties as may be termed physical properties, e.g. the property of a man's having ten fingers, two legs, two arms, \&c.; such properties are actually separable from the individuals who possess them, for they may be cut off without injuring the essence or even existence of such individuals: but this is not the case with other properties, which may be termed ideal properties: such properties have not any actual existence, and do not admit of any separation from the essence of which they are predicated; e.g, risibility in a man, and the having three angles in a triangle; and "such a property," Dr. Whately observes, "it is often hard to distinguish from the differentia; but whatever you consider as the most essential to the nature of a species, with respect to the matter you are engaged in, you must call the differentia; as rationality to man; and whatever you consider as rather an accompaniment (or result) of that difference, you must call the property; as the use of speech seems to be a result of rationality." And, note, (p. 73), "that the difference is not

[^17]:    ${ }^{\text {' }}$ It must be remembered, that the predicable and the c 2

[^18]:    - Summum genus, in its strictest sense, is that all-extensive term under which every object of whatever kind may be classed, and of every one of which it may be affirmatively predicated: the word which is generally used to denote such genus is substance, or, as some call it, being. Such is summum genus in its strict sense; but many other genera are frequently used as summa genera, according as may be most suitable to any particular science or system; thus, by an ornithologist, bird would be regarded as the summum genus under which he would arrange the different subdivisions of birds: so fish would be regarded as the summum genus most applicable to the study of ichthyology ; and this is the case with various other sciences.

    The general heads, or summa genera, to some of which we may refer every term, are denominated the categories, or predicaments; the doctrine of which was first taught by Archytas: they are generally considered as ten in number, viz. substance, quantity, quality, relation, place, time, situation, possession, action, suffering: the Greek terms which Aristotle has given them are as follows, ò̀ $i_{i \alpha}, \pi \delta \sigma o \nu, \pi o i ̂ o \nu, ~ \pi \rho \partial s ~ \tau \iota, \pi o \hat{,} \pi \delta \tau \epsilon$,
     may refer every term, according as may best suit our purpose, for the argument in which we may be engaged.

[^19]:    $k$ Generic properties may be predicated of many more individuals than specific properties, for the latter can be predicated only of the different individuals contained under one species, but generic properties may be predicated of different species, and consequently of all the individuals contained under those species. Thus the property, in triangles, that "the three angles are equal together to two right angles," is a generic property, and may be predicated of all triangles; but the property that "all equilateral triangles are also equiangular," is a specific property, and cannot be predicated of all triangles, but only of that species which is termed " equilateral."

[^20]:    $\times$ An individual cannot be defined but by description, i. e. by enumerating the accidents belonging to such individual, whereby the differences existing between that and any other may be shown.

[^21]:    The following table presents, at one view, the different kinds of definition, according to Aldrich's Logic :

[^22]:    c Judgement was defined (Part I. Sect. I.) to be " the decision upon the mutual agreement or disagreement of any two objects, when compared with each other;" and the sentence which declares this decision, and expresses judgement, is called " $a$ proposition:" now the agreement or disagreement of any two objects cannot be expressed in words, except by affirmation or negation; viz. by some assertion ; consequently it is necessary, in order to constitute a proposition, that it must be a sentence which affirms or denies : therefore its afirming or denying distinguishes it from any other kind of sentence, and is its difference.
    d Judgement is liable to the error of falsity, as has been shown before, (Part I. Sect. I.) for a decision may manifestly be false, inasmuch as it may have been decided that two particular objects agree when they do not, or vice versâ, and in such a case the decision or judgement would be false : hence a proposition which expresses such a decision must of necessity assert that which is not really the fact; i. e. it must signify that which is false: and since all propositions must either assert what is the fact, or what is not, consequently they must all signify something, either true or false ; and this is called a specific property of propositions, since it seems to result immediately from their difference, i. e. from their affirming or denying.

[^23]:    ${ }^{\text {h }}$ Modal propositions may be reduced to pure categoricals, by either considering the word which expresses the mode as united to the predicate, and thus forming a part of it; or sometimes by attaching it to the subject, which may be done when the mode only expresses whether the matter of the extremes be necessary, impossible, or contingent: e. g. "A fish necessarily lives in the water;" which means, "All fish live in the water;" "A profligate man may possilly repent and be saved;" viz. "The repentance and salvation of a profligate man is a thing that is possible."

[^24]:    1 The definitions which Aldrich has given of an affirmative proposition, viz. "that which has an affirmative copula;" and of a negative, viz. "that which has a negative copula." are accidental ; for the having an affirmative or negative copula, is not the differentia, but a property of such propositions; metaphysically they may be defined thus : affirmative propositions assert the agreement of their extremes, and negatives the disagreement : the copula serves to indicate this connexion. Care must be taken not to be deceived by the copula; for a proposition may have a negative in it without being a negative proposition : e.g. "He who is not wicked deserves our love," which is an affirmative proposition: the method of detecting this will be, to consider the meaning of the propositions, and what assertion is made relative to the extremes; if the proposition asserts that its extremes agree, it is affirmative, for agreement must be expressed by affirmation: but if it asserts that the extremes differ, it is negative; for negation alone expresses disagreement.

    D 2

[^25]:    ${ }^{1}$ A term is said to be distributed when it is taken in its fullest extent, i. e. when it is intended to comprehend everything to which it is applicable. Thus, "All misers are discontented;" the word " miser" is here distributed, for it is intended to comprehend every miser; and the proposition is equivalent to " there is not one miser who is not discontented :" but in the proposition, "Some men are avaricious," the word " men" is not distributed, because it is not intended to apply to every man; for there may be many men who are not avaricious.

[^26]:    - The quantity of propositions, as far as regards the words, is fourfold, viz. universal, particular, singular, and indefinite; but as far as it affects syllogistic argument, and, consequently, regards the judgment, which is expressed by it, it may be considered as of two kinds only, viz. universal and particular; for the singular (as has been shown) is equivalent to the universal, and the indefinite must be either universal or particular, according to the connexion which exists between its extremes, and which is termed the matter of a proposition. The word matter is an equivocal word, for it may signify either the component parts of a proposition, i. e. the subject, predicate, and copula, or the agreement or disagreement naturally subsisting between the subject and predicate, in which last sense it is here used.

[^27]:    p Propositions have been considered according to their substance, quality, and quantity; we now wish to find out of how

[^28]:    case, one of these propositions asserts the terms dogs and men to disagree universally, and the other asserts the partial agreement of these very same terms, employed in exactly the same sense with regard to each other: if therefore any one of these propositions be true, its contradictory must be false; and if false, its contradictory must be true.

[^29]:    ₹ To discover the matter of any proposition cannot be effected by logic, but depends upon the science or system to which the subject matter of the proposition belongs; thus, "The planets are not stationary;" the extremes of this proposition are asserted to differ; and this assertion will evidently be true, if these extremes really do differ; this point, however, could not be discovered by logic ; but rather from a knowledge of astronomy, to which science the subject matter belongs.

[^30]:    ${ }^{d}$ If any proposition, in which one term only was distributed, were simply converted, it is manifest that, after conversion, the other term would be distributed ; and since, by the hypothesis, this term could not have been distributed before, such conversion cannot be illative : hence it follows, that (unless under some accidental circumstances) neither $A$ nor $O$ can be simply converted.

[^31]:    ${ }^{\text {a }}$ The principles, from the truth of which the conclusion is drawn, are supposed to be known, "quasi sine discursu;" as Aldrich observes, (chap. iii. $\$ 1$.), at least they must be laid down as hypothetically true; i.e. they must " antecedere" or " præmitti;" for which reason they are termed the antecedent, or the premises.

    The inference follows from the force of the premises; hence it is said to be concluded, inferred, collected, or deduced from them.

[^32]:    e For, as Aldrich observes, (chap. iii. § 1.), "Mutatis terminis, et servatâ eorum dispositione, Materialis plerumque fallit, Formalis semper obtinet." Since the material consequence depends entirely upon the power or meaning of the terms, if these terms be changed, the consequence will not hold good, at least it will not result necessarily; but in the formal consequence the inference does result necessarily; and this will stand good, even though the terms be changed, if their order be preserved; and although a conclusion may be false, if the terms be changed, yet

[^33]:    (The premises must either be known to be true, or be proved to be so, before any inference can be drawn from them. Logic undertakes to ascertain the validity of an argument, only so far as the form of expression is concerned. The premises, therefore, (in all the examples which may be adduced in this treatise), will be considered as hypothetically true, unless where the contrary is particularly specified.
    $g$ The conclusion or consequent is frequently, in common conversation, stated before the premises; this may also be observed in most authors: in such a case the antecedent is connected

[^34]:    k Thus, let there be two terms, " Men" and "Plants;" and since no third term can be adduced which will agree with both these terms, it will consequently be impossible to prove their agreement ; i. e. to prove that " Men are plants."
    ${ }^{1}$ Again, let there be the two terms, " animal," and " sensitive being :" there is not any idea comprised in the one which is not also comprised in the other ; therefore they must entirely agree with each other, for in this case no third term could be adduced with which one of these terms would agree, and from which the other could differ.

[^35]:    ${ }_{m}$ The categories which have been mentioned above, [see p. 31, note h], " will serve (as Dr. Whately observes) the purpose of marking out certain tracks, as it were, which are to be pursued in searching for middle terms in each argument respectively; it being essential that we should generalize on a right principle, with a view to the question before us; or, in other words, that we should abstract that portion of any object presented to the mind which is important to the argument in hand."-Elements of Logic.

[^36]:    $\sqrt{\text { " Hector slew Patroclus ;" }}$
    " Achilles slew Hector:"
    "Achilles slew Patroclus."

[^37]:    n If the terms of these propositions were written at full length, the utter want of connexion between the two premises would be more apparent:
    " Hector was the person who slew Patroclus:"
    " Achilles was the person who slew Hector."
    These two propositions have no connexion with each other, but are two distinct and wholly unconnected assertions; consequently no inference could be deduced from them.

    - As there are but three terms which are to be compared together, i. e. the major, minor, and middle, it is manifest, that

[^38]:    ${ }^{r}$ This rule is evidently but a branch of the first; for an ambiguity of the middle will, in all cases, be equivalent to employing two middle terms; and thus the extremes would not be compared with one and the same third, which, as was before shown, is necessary to be done: all equivocal words will produce this kind of ambiguity; e.g.
    " A club is a society of men;"
    "A thick stick is a club:"
    therefore, " A thick stick is a society of men."
    Again:-The following apparent argument contains four terms, because of the ambiguity of the middle.
    " That which peculiarly characterizes man from any other animal, is the faculty which he possesses of roasting eggs ; for the peculiar characteristic of man is reason, and there is reason in roasting eggs."

[^39]:    - The first canon is, that when two terms both agree with one and the same third term, they agree with each other: now this cannot be shown to be the case, unless that third term be once taken in its most extensive signification; for if one extreme agrees with all the middle, and the other with a part of it, they do in fact agree with the same term, and therefore agree with each other : and this may be shown by the following argument, which will be true, provided it be admitted that the same part of the middle is compared with both extremes; e. g.
    " All metals are fusible;"
    " Lead is fusible:"
    therefore, " Lead is a metal."

[^40]:    $\times$ Let any two terms both differ from another third, these terms cannot be said to agree together; for, if so, they would both agree with the third: neither can it be inferred that they differ from each other; for in such a case, one would agree with the third term, and the other differ from it; and both these cases are contrary to the hypothesis.

[^41]:    - These twelve rules are wholly founded upon the two first syllogistic canons; consequently recourse must be had to these canons, in order to prove any one of them; and when any violation of these rules takes place, there is not, in reality, any comparison made of the two extremes with one and the same third term, with which they both agree, or with which one agrees, and from which the other differs.

[^42]:    k See Aldrich, chap. iii. \& 4.
    ${ }^{1}$ Thus the following argument is incorrect:-
    $\sqrt{ }$ " Some learned men are much addicted to prejudice ;"
    " None who are much addicted to prejudice are men of powerful minds:"
    therefore, " Some men of powerful minds are not learned:" for in this apparent syllogism, there is an illicit process of the major term, " learned :" and this must be the case, however the order of the terms of the argument be changed, viz. in every figure; hence this mood is necessarily and essentially incorrect.

[^43]:    n By means of this scheme, it will be easy to discover in what figure any syllogism may be, as well as to make a syllogism in any particular figure, by determining the quantity and quality of the different propositions, and by taking care not to violate any one of the twelve rules given in the last section.

[^44]:    PThus, AAI, IAI, and EAO, are allowable in the third and fourth, and EIO in all the figures; hence it would be impossible to designate the particular figure by mentioning the vowels only, which constitute the mood; besides, these names are of great use in reduction, as will be seen hereafter.

    9 Whatever mood has an universal conclusion, must of course contain a nameless mood under it; and since there cannot be more than five moods, in which an universal conclusion can be inferred from universal premises; (viz Barbara, Celarent, Cesare, Camestres, and Camenes,) hence it is obvious, that there cannot be more than five nameless moods; viz, one under each, AAI and EAO in the first figure, EAO and AEO in the second, and AEO in the fourth.

[^45]:    s The case is exactly similar where the conclusion is negative; e.g.
    " No man can serve two masters;"
    "You are a man:"
    therefore, " You cannot serve two masters."
    Here the major term is negatively predicated of the middle distributed; therefore it can be negatively predicated of any term comprehended by that middle; but in the minor premiss it is asserted, that the minor is comprehended under the middle; hence the major can be negatively predicated of the minor.

[^46]:    t They are also called "perfect," because nothing more is implied in the premises, than is necessary to prove the conclusion, which is not the case with the other moods, which are therefore termed "imperfect."

    - See Aldrich, chap. iii. § 6.

[^47]:    x There are two modes by which all conclusions may be proved, viz the direct and the indirect. The direct mode is where the original conclusion is shown to be true, by placing those principles (from which it is deduced) in such a manner that the conclusion results from them necessarily; so that the mind cannot but immediately admit the truth of the conclusion, after having admitted the truth of the premises. The indirect mode is that in which the conclusion is assumed to be false, and then showing that from this assumption some palpable absurdity must result; the necessary consequence of this is, that the assumption must be false: hence the conclusion (which was pro formâ assumed false) must in reality be true. The latter of chese modes generally strikes the student's mind most forcibly, and is in most cases the easiest. Thus, in order to prove any rule, the best way is to viobste the rule, and trace the consequences of such violation to their source: the result will then become apparent, and the validity of the rule will be established.

[^48]:    $y$ Dr. Whately has shown that all the imperfect moods may be reduced ostensively : the two moods which are usually reduced by reductio ad impossibile, and which are called Baroko and Bokardo, he has changed to Fakoro and Dokamo ; and he has shown that they may be reduced ostensively by means of conversion by contraposition, (see Part II. Sect. V.) I will take his own example in Baroko:
    $\checkmark$ " Every true patriot is a friend to religion ;"
    " Some great statesmen are not friends to religion :"
    "Some great statesmen are not true patriots:"
    reduced to Ferio, by converting the major by negation, (contraposition,) thus:
    $\checkmark$ " He-who-is-not-a-friend-to-religion is not a true patriot;"
    " Some great statesmen are not-friends-to-religion:"
    " Some great statesmen ape not true patriots."
    In the same manner he has shown that Bokardo may be reduced ostensively to Darii, by converting the major premiss by contraposition, and then transposing the premises.

[^49]:    $z$ It must be remembered that these letters are intended to apply to the vowels which precede, and not to those which follow them : thus, in Datisi the minor premiss is to be simply converted, and not the conclusion; and in like manner with all the other moods: so also the letter $k$ applies to the preceding vowel in Baroko and Bokardo, and not to the vowel that follows it.

    * All imperfect moods, although their conclusions are true, are forced to imply more than they express in their premises, in order to prove the necessity of their conclusions: thus, in Ferison, e.g.

    M' No Mahometans are Christians;"
    " Some Mahometans are men of good understanding:"
    therefore, " Some men of good understanding are not Christians."

[^50]:    " All acts which deserve reward are duly rewarded;"
    " All good acts deserve reward:"
    therefore, " All good acts are duly rewarded."
    This new conclusion must be false, because it contradicts the original major premiss; therefore the major premiss from which it was drawn, must be false; therefore its contradictory (which is the original conclusion) must be true.

[^51]:    " Some high-bred horses are not fleet;"
    " All racers are high-bred:"
    therefore, " Some racers are not fleet."

[^52]:[^53]:    $\times$ Dr. Whately has shown that, beginning at the conclusion, it will appear that the major term seems to be predicated of itself: thus, the major is predicated of the minor, the minor of the middle, and the middle of the major ; i. e. apparently the major is predicated of itself.

    5 This will be more manifest if expressed thus shortly : the middle is predicated of the major, the major of the minor, and the minor of the middle; thus it is implied, that the middle is predicated of the middle : this must of course be superfluous, and it is principally on this account that the fourth figure appears so unnatural; for the conclusion does not seem to result necessarily from the premises; hence it is scarcely ever used in argument : in fact, it is of no practical use whatsoever.

[^54]:    f It is by induction that all axioms are known, such as, " Things that are equal to the same are equal to each other ;" " A whole is greater than its parts;" and all other mathematical axioms: whence it may be observed, that induction is that mode of argument which is adapted to the discovery of any principles or facts which are not previously known. Thus, Aristotle, in his Ethics, proves by induction that all virtue: consists in a mean; for he shows that this is the fact with respect to each of the virtues, which he enumerates, and consequently infers the universal conclusion with respect to them all.

[^55]:    t The inference drawn by example sometimes is such as produces but a small degree of probability; for fables, similes, and allegories, are comprehended under it. It is called by Aristotle, "oratorial induction." Artabanus makes use of this kind of argument when endeavouring to dissuade Xerxes from invading Greece, saying, that Darius had failed in his expedition against the Scythians, and that the Grecians were more warlike men than the Scythians, consequently that his expedition would probably be attended with more dangerous consequences than the expedition of Darius.

    This mode of argument is very frequently employed; indeed it is almost the only mode which, under many circumstances, it is possible to adopt, such as in contingencies, which might not admit of any positive proof: in such cases, it should be remembered, that the greater the number of facts is, which are adduced in support of the subject in question, the greater will be the degree of probability of its occurrence.

[^56]:    1 The conclusion of an argument is supposed to be known by means of the question, or problem, which is to be proved; hence formally to state the conclusion at the close of an argument, would be of no use, and would only produce tautology.

    - See Aldrich, chap. iii. § 9 .

